

1 **An Improved Algorithm for Estimating the Secchi Disk Depth from Remote**
2 **Sensing Data Based on the New Underwater Visibility Theory**

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21

22 **Abstract**

23 The Secchi disk depth (Z_{SD}) is a widely used parameter for evaluating water clarity. Here we
24 propose an improved algorithm, which is based on a new underwater visibility theory, for
25 retrieving more accurate Z_{SD} from remote sensing reflectance (R_{rs}) in various waters. Two
26 improvements were carried out in the new algorithm. First, we used a hybrid quasi-analytical
27 algorithm (QAA_hybrid) instead of the sixth version of QAA (QAA_v6) for retrieving more
28 accurate total absorption coefficient ($a(\lambda)$) and total backscattering coefficient ($b_b(\lambda)$) even in
29 turbid inland waters. Second, we used a dynamic K_T/K_d ratio (i.e., ratio of diffuse attenuation
30 coefficient of upwelling radiance and diffuse attenuation coefficient of downwelling irradiance)
31 instead of using the fixed ratio (i.e., 1.5). The results obtained from in situ R_{rs} show that the
32 improved Z_{SD} estimation algorithm gave more accurate Z_{SD} estimations, with the root mean
33 square error (RMSE) reduced from 0.2 to 0.1 in log10 unit, mean absolute percentage error
34 (MAPE) reduced from 39 % to 20 % (N=178 with in situ Z_{SD} values between 0.3 – 20.8 m). We
35 then applied the improved Z_{SD} estimation algorithm to the 2003–2012 MERIS images for Lake
36 Kasumigaura to further confirm the performance of the improved Z_{SD} estimation algorithm. The

37 results obtained from 19 matchups demonstrate that the estimated Z_{SD} matched well with the in
38 situ Z_{SD} , with the RMSE of 0.11 m and the MAPE of 15%. The improved Z_{SD} estimation
39 algorithm shows a potential to estimate more accurate Z_{SD} values from remote sensing data in
40 various waters.

41 **Keywords:** Secchi disk depth, quasi-analytical algorithm, remote sensing, various waters, hybrid

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55 **1. Introduction**

56 The Secchi disk depth (Z_{SD}), also termed 'water clarity' or 'transparency' in aquatic
57 sciences, is a direct record of water optics and an important indicator of water quality (Wernand
58 et al., 2010). Therefore, the Z_{SD} has been a routine measurement in field survey of aquatic
59 environments using a called Secchi disk since the 1860s (Secchi, 1864). Over a century later, the
60 remote sensing technique has also been widely used for retrieving the Z_{SD} values because of the
61 technique's large area coverage and rapid data acquisition (Yarger and McCauley, 1975; Carlson,
62 1977). Generally, there are two approaches for retrieving the Z_{SD} from remote sensing data:
63 empirical and semi-analytical approaches. The empirical approach usually estimates the Z_{SD} by
64 directly carrying out a regression analysis between the remote sensing data and in situ Z_{SD}
65 measurements (e.g., Giardino et al., 2001; Kloiber et al., 2002; Kratzer et al., 2003; Chen et al.,
66 2007; Olmanson et al., 2008; Kabbara et al., 2008; Kratzer et al., 2008; Zhao et al., 2011;
67 Olmanson et al., 2016).

68 In contrast, the semi-analytical approach retrieves the Z_{SD} based on an underwater
69 visibility theory (Doron et al., 2011; Fukushima et al., 2016, 2018; Alikas and Kratzer, 2017;
70 Rodrigues et al., 2017). Compared to the empirical approach, the semi-analytical approach has
71 two advantages: (1) a clearer mechanism and thus more reliable results; and (2) this approach
72 often does not need in situ data for recalibrating the retrieval algorithm. It can thus be considered

73 that the semi-analytical approach would be more useful for monitoring the Z_{SD} in various water
74 bodies, especially for those that lack in situ measurements.

75 Before 2015, semi-analytical algorithms for Z_{SD} retrieval were based mainly on an
76 underwater visibility theory proposed by Duntley (1952) (hereafter referred to as the 'classical
77 theory'). According to the classical theory, the Z_{SD} is inversely proportional to the sum of the
78 beam attenuation coefficient (c , m^{-1}) and the diffuse attenuation coefficient of downwelling
79 irradiance (K_d , m^{-1}) within the visible domain (Tyler, 1968; Preisendorfer, 1986). However, Lee
80 et al. (2015a, 2018) pointed out that there are some drawbacks or mistakes in the classical theory,
81 which has been used for more than 60 years. First, the critical assumption, i.e., that the radiance
82 distribution over the target is equal to the radiance distribution over the background, may not be
83 valid for water bodies because a 30-cm Secchi disk cannot be treated as a point at a distance
84 shorter than tens of meters. Second, the use of full visible domain to determine a Z_{SD} value is not
85 appropriate because how far the human eye-brain system is able to see should depend on
86 information from a visible wavelength with maximum transmittance in a water body. Third, the
87 use of relative difference between water and Secchi disk just match the sharpness of an object,
88 which is not the case of using a 30-cm Secchi disk to measure Z_{SD} within tens of meters.

89 To overcome the above problems, Lee et al. (2015a) proposed a new theory for underwater
90 visibility (hereafter referred to as the 'new theory'). Based on this new theory, Lee et al. also

91 developed a semi-analytical algorithm for retrieving the Z_{SD} from remote sensing data (hereafter
92 referred to as the 'Lee15'). The Lee15 algorithm is comprised of three main steps: (1) retrieving
93 the total absorption coefficient $a(\lambda)$ and the total backscattering coefficient $b_b(\lambda)$ from the
94 remote sensing reflectance $R_{rs}(\lambda)$ by using the sixth version of the quasi-analytical algorithm
95 (QAA_v6, Lee et al., 2002; IOCCG, 2014); (2) calculating the $K_d(\lambda)$ from $a(\lambda)$ and $b_b(\lambda)$ as
96 well as the corresponding solar zenith angle by using a semi-analytical model developed by Lee
97 et al. (2005, 2013); and (3) estimating the Z_{SD} from the selected minimum K_d and the
98 corresponding R_{rs} at the visible bands.

99 However, several research groups have reported that the QAA_v6 or its previous version
100 (QAA_v5) often failed in turbid inland waters (Le et al., 2009; Yang et al., 2013; Huang et al.,
101 2014; Mishra et al., 2014; Watanabe et al., 2016; Wang et al., 2017). It can be speculated that the
102 estimation errors of $a(\lambda)$ and $b_b(\lambda)$ will be propagated to the estimations of $K_d(\lambda)$ and then the
103 final estimations of the Z_{SD} . Some of the above-cited groups also sought to modify the QAA_v6
104 or QAA_v5 for obtaining more accurate $a(\lambda)$ and $b_b(\lambda)$ values in turbid inland waters. It is
105 thus necessary to integrate these new endeavors into the Lee15 algorithm to improve its
106 applicability for various water bodies around the world.

107 Another potential error source in the Lee15 algorithm is the assumption of a constant ratio
108 of the upwelling radiance diffuse attenuation coefficient (K_T) and K_d . Empirically, the ratio value

109 of 1.5 was used in the Lee15 algorithm (i.e., $K_T = 1.5K_d$). However, a wide range of ratios have
110 been reported (0.5–2.0). For example, Philpot (1989) pointed out that the reasonable range for
111 K_T/K_d was from 0.5 to 2. Maritorena et al. (1994) reported that K_T/K_d ranged from 1.02 to
112 1.66 based on simulations. A K_T/K_d range of 1.4–1.7 can also be estimated when the solar
113 zenith angle $\theta = 0$ degrees according to Lee et al. (1994). It can thus be speculated that using a
114 fixed K_T/K_d value in a Z_{SD} estimation may lead to errors, and more realistic K_T/K_d ratios are
115 needed to further improve the performance of the Lee15 algorithm.

116 We therefore conducted the present study to: (1) improve the Lee15 algorithm for
117 estimating the Z_{SD} values in various waters by integrating different types of QAAs and dynamic
118 K_T/K_d ratios into the original algorithm, and (2) evaluate the performance of the improved
119 Lee15 algorithm using in situ data collected from several Japanese lakes and SeaBASS dataset as
120 well as MERIS (MEDium Resolution Imaging Spectrometer) data over Lake Kasumigaura,
121 Japan.

122

123 **2. Study Area and Data Collection**

124 2.1. Study area

125 The study area of this research included 8 lakes in Japan (Fig. 1a) and coastal waters in
126 United States. The 8 Japanese lakes include Lakes Biwa, Kasumigaura, Akan, Suwa, Motosu, Sai,

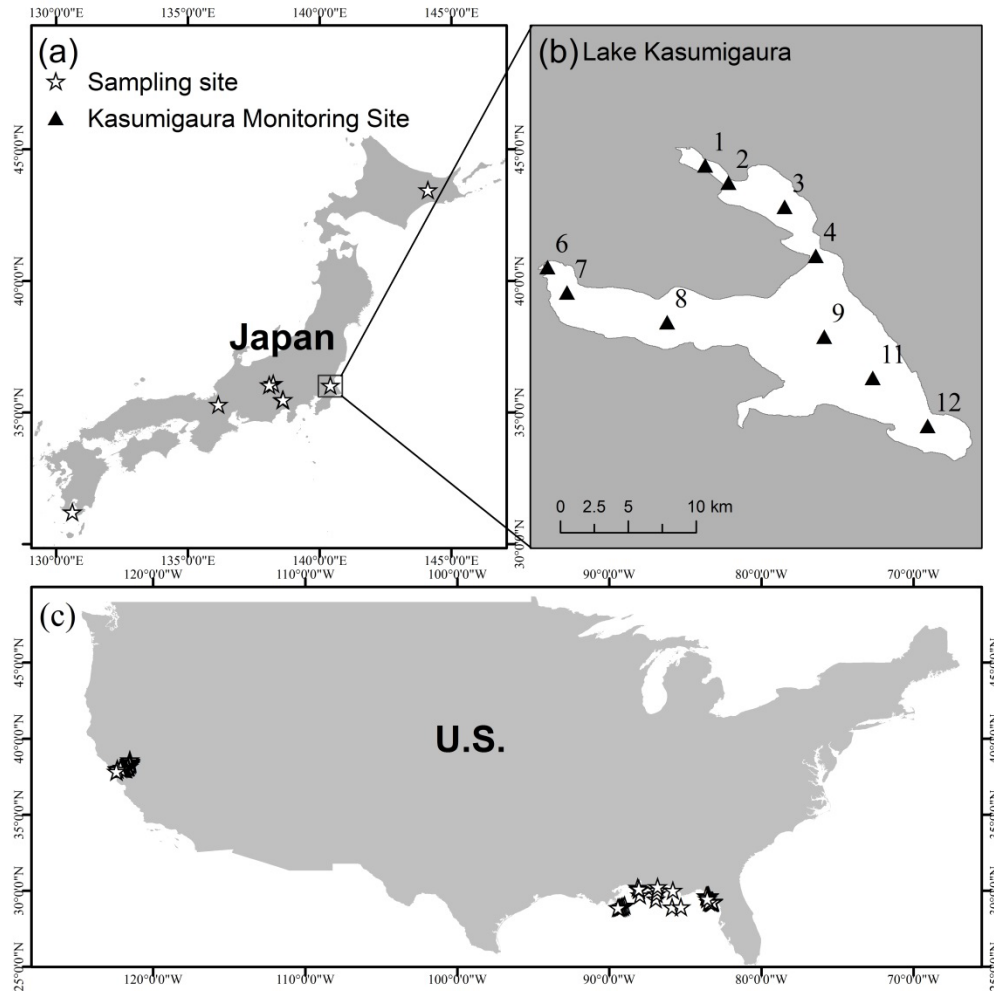
127 Unagi, and Shirakaba. The water quality parameters of these lakes varied widely, with Z_{SD} values
 128 from 0.4 m to 16.4 m, chlorophyll-a concentrations ranging from 0.5 mg/m³ to 148.6 mg/m³, and
 129 total suspended solids (TSS) ranging from 0.4 g/m³ to 45.6 g/m³ (Table 1). The coastal waters in
 130 United States include San Francisco Bay and the northern Gulf of Mexico (Fig.1c). In total 129
 131 in situ-measured R_{rs} spectra with corresponding Z_{SD} were collected from the SeaBASS dataset,
 132 and the Z_{SD} values ranged from 0.3 m to 20.8 m.

133 Lake Kasumigaura, with a surface area of 220 km² and a mean water depth of 4 m, was
 134 also used for MERIS data analyses (Fig. 1b). Its Z_{SD} values ranged from 0.4 m to 1.2 m. The
 135 chlorophyll-a concentration ranged from 12.0 mg/m³ to 148.6 mg/m³ and the TSS ranged from
 136 4.1 g/m³ to 45.6 g/m³ in this lake. There are 10 routine monitoring sites in Lake Kasumigaura
 137 with a monitoring frequency of 1 month.

138

139 **Table 1.** Area, depth, water quality, and number of collected data of 8 Japanese studied lakes

Lake name	Area (km ²)	Maximum depth (m)	Z_{SD} (m)	Chl-a (mg/m ³)	TSS (g/m ³)	Number of data
Biwa	670.3	103.8	3.2-9.3	0.7-2.9	0.6-2.0	15
Kasumigaura	220.0	11.9	0.4-1.2	12.0-148.6	4.1-45.6	77
Akan	13.0	44.8	6.7	0.8	1.5	1
Suwa	12.9	7.6	0.9-1.9	9.8-29.4	4.6-9.6	16
Motosu	4.7	121.6	16.4	0.6	0.4	1
Sai	2.1	71.7	6.8-7.1	1.8	1.3	2
Unagi	1.2	55.8	12.8	0.5	0.4	1
Shirakaba	0.4	9.1	3.5	2.3	2.8	1



140

141 **Fig. 1.** Study area. (a) Field samplings were carried out in 8 lakes in Japan. (b) Lake

142 Kasumigaura (only western part is shown) and its 10 routine monitoring sites. (c) Sampling sites

143 of data collected from SeaBASS.

144 2.2. In situ data collection and processing

145 Field surveys were carried out in the 8 above-described Japanese lakes during 2009–2016.

146 Data were collected from a total of 114 sampling sites. For each site, the Z_{SD} was measured by

147 vertically lowering down a 30-cm-dia. white disk into the water until the disk was no longer

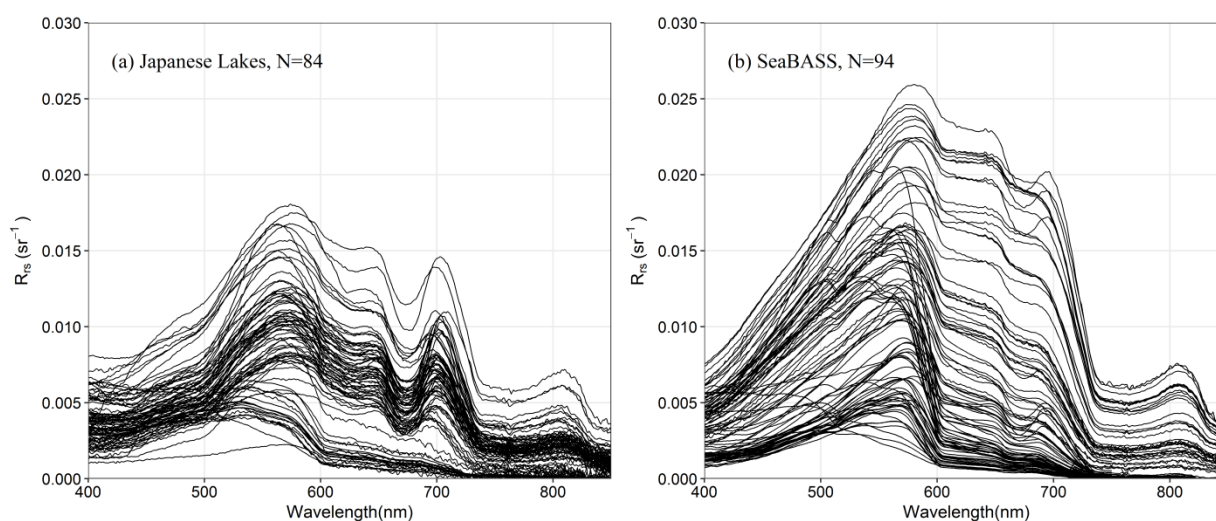
148 visible (or lower a Secchi disk out of sight and then raise the disk until it becomes visible). At the
149 same time, the radiance of skylight (L_s), the radiance from a standard gray board (L_g), and the
150 total upwelling radiance from the water (L_t) were measured using a FieldSpec® HandHeld
151 spectroradiometer (ASD Inc., Boulder, CO, USA) between the local time 9:30 to 14:00 (three
152 measurements between 14:00 and 16:00), with the sensor zenith angle of 40° and azimuth angle
153 of 135° from the sun.

154 Remote sensing reflectance (R_{rs}) was then calculated using the following equation:

$$155 \quad R_{rs} = (L_t - \rho L_s) / \left(\frac{\pi}{R_g} L_g \right) - \Delta \quad (1)$$

156 where ρ is the skylight reflectance (0.028 when the wind speed was <5 m/sec, Mobley, 1999),
157 and R_g is the reflectance of the gray board; Δ is the contribution of the residual reflected skylight,
158 which was calculated from the median R_{rs} value between the wavelengths of 950 and 1000 nm
159 for turbid water and 800–850 nm for clear water. This is because the absorption coefficient of
160 pure water is extremely high (it can reach 48 m^{-1}) at the wavelengths of 950–1000 nm (Kou et
161 al., 1993), and thus the R_{rs} at these wavelengths can be reasonably assumed as 0 sr^{-1} . For the R_{rs}
162 spectra obtained from SeaBASS, we only downloaded those data marked as 'final' status, which
163 indicate the R_{rs} spectra have been preprocessed (including the correction of residual reflected
164 skylight). The quality of all R_{rs} spectra (including 114 spectra from Japanese lakes and 129
165 spectra from SeaBASS) was checked using a method proposed by Wei et al. (2016), which is a

166 quality assurance (QA) system for providing a score between 0 (unusable) and 1 (perfect) to each
167 R_{rs} spectrum to objectively evaluate its quality. In this study, only the R_{rs} spectra with quality
168 scores larger than 0.8 were used for Z_{SD} estimations. Figure 2 shows the final remained R_{rs}
169 spectra (84 from Japanese lakes, 94 from SeaBASS). All selected R_{rs} spectra were then converted
170 to MERIS bands based on the MERIS Spectral Response Functions.



171
172 Fig.2. R_{rs} spectra used in this study. (a) 84 R_{rs} spectra collected from 8 lakes in Japan. (b) 94 R_{rs}
173 spectra collected from SeaBASS.

174 For 8 Japanese lakes, water samples were collected and kept in ice boxes, and taken to the
175 laboratory immediately after finishing the collection. The absorption coefficients of
176 phytoplankton ($a_{ph}(\lambda)$), tripton ($a_{tr}(\lambda)$) and CDOM ($a_{CDOM}(\lambda)$) were measured following the
177 NASA protocols (Mitchell et al., 2002). The total absorption coefficient $a(\lambda)$ was calculated as
178 the sum of $a_{ph}(\lambda)$, $a_{tr}(\lambda)$, $a_{CDOM}(\lambda)$, and the absorption coefficient of pure water, i.e.,

179 $a_w(\lambda)$. The values of $a_w(\lambda)$ were taken from Lee et al. (2015b), Pope and Fry (1997), and Kou
180 et al. (1993). In total, $a(\lambda)$ values at 52 sites from Lakes Suwa and Kasumigaura were
181 collected.

182 In several Japanese lakes (Lakes Shirakaba, Unagi, Sai, Biwa, Suwa and Kasumigaura),
183 the downward irradiance (E_d) at 443 nm, 555 nm, and 669 nm at different depths of the water
184 column was also measured using a Multispectral Radiometer (Satlantic, Halifax, Canada). These
185 data were used to obtain the measured K_d and then compared with R_{rs} -derived K_d at these
186 wavelengths. In total, the measured K_d values at 99 sites were collected.

187 We also obtained the in situ Z_{SD} data measured between 2003 and 2012 from the Lake
188 Kasumigaura Database, which was published by the National Institute for Environmental Studies,
189 Japan (NIES, 2016; referred to hereafter as the 'NIES-dataset'). This database provides monthly
190 Z_{SD} values at 10 sites in Lake Kasumigaura (the monitoring sites shown in Fig. 1b). We used
191 these data to evaluate the performance of the proposed algorithm by using actual satellite images.
192 For more appropriate comparison, we corrected variations of visibility due to changes in the
193 solar zenith angle for these in situ-measured Z_{SD} values using a method proposed by Verschuur
194 (1997).

195 2.3. Satellite image pre-processing

196 We used MERIS data in this study because of its higher spatial (300 m) and temporal (3

197 days') resolutions. All available MERIS images covering Lake Kasumigaura from 2003 to 2012
198 were downloaded from the European Space Agency (ESA, <https://www.esa.int/ESA>). The
199 downloaded images were first clipped to the Lake Kasumigaura area, and then radiometric
200 correction was performed to remove the smile-effect.

201 We used the Case-2 Regional Processor in the BEAM 5.0 Earth Observation Toolbox and
202 Development Platform (Brockmann Consult, Geesthacht, Germany) to perform atmospheric
203 correction. Clouds, cloud shadows, cloud buffers and coastal lines were then detected using the
204 Idepix algorithm in the Sentinel Application Platform 6.0 (SNAP). Finally, the pixels with failed
205 atmospheric correction, clouds, cloud shadows, cloud buffers, or land and coastal lines were
206 masked out. A total of 200 images remained for the Z_{SD} estimation.

207 For all **MERIS-derived** Z_{SD} values, we firstly corrected variations of visibility due to
208 changes in the solar zenith angle using Verschuur's method (Verschuur, 1997). We then averaged
209 all daily estimated Z_{SD} values in the same month to generate monthly estimated Z_{SD} values.
210 Finally, a temporal trend analysis was carried out for both monthly measured and estimated Z_{SD}
211 values during the study period using a linear regression method, which has been widely used in
212 previous studies (e.g., Shang et al., 2016).

213 **Matchups were generated to compare MERIS-derived Z_{SD} values and the in situ-measured**
214 **Z_{SD} values from NIES-dataset (acquired on the same day).** A 3×3 window was used to extract the

215 estimated Z_{SD} values from the MERIS images, and we used the averaged Z_{SD} estimations for the
 216 comparison to mitigate effects due to imperfect geometric corrections.

217

218 **3. Development and Assessment of the Z_{SD} Retrieval Algorithm**

219 3.1. The original Lee15 algorithm

220 The original Lee15 algorithm contains three main steps. First, QAA_v6 is used to retrieve
 221 $a(\lambda)$ and $b_b(\lambda)$ from $R_{rs}(\lambda)$. In the QAA_v6, if $R_{rs}(670) < 0.0015 \text{ sr}^{-1}$, 560 nm is used as
 222 the reference band (i.e., QAA_v5), otherwise the reference band is shifted to 670 nm. Second,
 223 $K_d(\lambda)$ is estimated from $a(\lambda)$ and $b_b(\lambda)$ using the following equation (Lee et al., 2005,
 224 2013):

$$225 \quad K_d(\lambda) = (1 + 0.005\theta)a(\lambda) + 4.259 \left(1 - 0.265\eta_w(\lambda)\right) \left(1 - 0.52e^{-10.8a(\lambda)}\right)b_b(\lambda) \quad (2)$$

226 where θ is the solar zenith angle, $\eta_w(\lambda)$ is the ratio of $b_{bw}(\lambda)$ (the backscattering coefficient
 227 of pure water, Morel, 1974; Zhang et al., 2009) and $b_b(\lambda)$. Finally, the Z_{SD} is estimated from
 228 $K_d(\lambda)$ and the corresponding $R_{rs}(\lambda)$ using the following equation based on the new underwater
 229 visibility theory (Lee et al., 2015a):

$$230 \quad Z_{SD} = \frac{1}{2.5\text{Min}(K_d(\lambda))} \ln \left(\frac{|0.14 - R_{rs}^{PC}|}{C_t^r} \right) \quad (3)$$

231 where $\text{Min}(K_d(\lambda))$ is the minimum K_d value among the visible bands, R_{rs}^{PC} is the
 232 corresponding R_{rs} at the band with the minimum K_d , and C_t^r is the contrast threshold for

233 sighting a white disk (i.e., 0.013 sr^{-1}). The coefficient of 2.5 was obtained under an empirical
234 assumption of $K_T = 1.5K_d$.

235 3.2. Improving the Lee15 algorithm for Z_{SD} retrieval in a variety of water bodies

236 We carried out two improvements for the original Lee15 algorithm. First, by considering
237 the shortcoming of QAA_v6 in turbid waters, we proposed the use of another QAA, which was
238 specifically developed for turbid inland waters by Yang et al. (2013), to estimate $a(\lambda)$
239 and $b_b(\lambda)$ in this type of waters (hereafter referred to as the 'QAA_T'). We selected the
240 QAA_T algorithm in this study because all of the equations in the QAA_T are semi-analytical or
241 analytical equations without any in situ data used for recalibration (Yang et al., 2013).

242 For clear waters, we still used QAA_v5 because of its good performance in this type of
243 waters (Lee et al., 2002; Fukushima et al., 2016). We adapted the maximum chlorophyll-a index
244 (MCI) originally developed by Gower et al. (2005) for switching the QAA_v5 and QAA_T. The
245 modified MCI is defined as (Matsushita et al., 2015):

$$246 \quad MCI = R_{rs}(709) - R_{rs}(665) - \left[\frac{(709-665)}{(754-665)} (R_{rs}(754) - R_{rs}(665)) \right] \quad (4)$$

247 where $R_{rs}(665)$, $R_{rs}(709)$ and $R_{rs}(754)$ are the remote sensing reflectance at 665 nm, 709
248 nm and 754 nm, respectively. According to Matsushita et al. (2015), $MCI = 0.0016 \text{ sr}^{-1}$ was used
249 to distinguish clear and turbid waters. We named this blended QAA as 'QAA_hybrid', and its
250 main steps are summarized in Table 2.

251 **Table 2.** Main steps of the QAA_hybrid

Step	Property	Derivation
1	$r_{rs}(\lambda)$	$r_{rs}(\lambda) = R_{rs}(\lambda)/(0.52 + 1.7R_{rs}(\lambda))$
2	$u(\lambda)$	$u(\lambda) = \frac{-0.089 + \sqrt{0.089^2 + 4 \times 0.125r_{rs}(\lambda)}}{2 \times 0.125}$
3	MCI	$MCI \leq 0.0016 \text{ sr}^{-1}$ (QAA_v5) $MCI > 0.0016 \text{ sr}^{-1}$ (QAA_T)
4	$a(\lambda_0)$	$x = \log\left(\frac{r_{rs}(443) + r_{rs}(490)}{r_{rs}(560) + 5\frac{r_{rs}(670)}{r_{rs}(490)}r_{rs}(670)}\right)$ $a(560) = a_w(560) + 10^{-1.146 - 1.366x - 0.469x^2}$ $a(754) = a_w(754)$
5	$b_{bp}(\lambda_0)$	$b_{bp}(560) = \frac{u(560) \times a(560)}{1 - u(560)} - b_{bw}(560)$ $b_{bp}(754) = \frac{u(754) \times a(754)}{1 - u(754)} - b_{bw}(754)$
6	$b_{bp}(\lambda)$	$Y = 2.0 \left(1 - 1.2 \exp\left(-0.9 \frac{r_{rs}(443)}{r_{rs}(560)}\right) \right)$ $b_{bp}(\lambda) = b_{bp}(560) \left(\frac{560}{\lambda}\right)^Y$ $Y = -372.99\beta^2 + 37.286\beta + 0.84$ $\beta = \log[u(754)/u(779)]$ $b_{bp}(\lambda) = b_{bp}(754) \left(\frac{754}{\lambda}\right)^Y$
7	$a(\lambda)$	$a(\lambda) = (1 - u(\lambda))(b_{bw}(\lambda) + b_{bp}(\lambda))/u(\lambda)$

252 Our second improvement for the Lee15 algorithm was to develop another algorithm for
 253 estimating a more realistic ratio of K_T and K_d in various waters. According to previous studies,
 254 the subsurface remote sensing reflectance (r_{rs}) at optically shallow waters can be expressed as
 255 follows (Philpot, 1989; Maritorea et al., 1994; Lee et al., 1998):

$$256 \quad r_{rs} \approx r_{rs}^{dp} \{1 - A_0 \exp[-(K_d + K_u^C)H]\} + A_1 \rho \exp[-(K_d + K_u^B)H] \quad (5)$$

257 where r_{rs}^{dp} is the r_{rs} for optically deep waters, A_0 is 1.0, and A_1 is $1/\pi$ for a lambertian bottom,
 258 K_u^C is the diffuse attenuation coefficient of upwelling radiance from the water column scattering,
 259 K_u^B is the diffuse attenuation coefficient of upwelling radiance from the bottom, ρ is the bottom
 260 reflectance, and H is the bottom depth. The first term on the right side of the equation refers to

261 the reflectance from the water column, and the second term on the right refers to the reflectance
 262 from the bottom. According to Lee et al. (1999) and Barnes et al. (2018), K_d and K_u^B can be
 263 estimated using the following equations:

$$264 \quad K_d = D_d \alpha \approx [1/\cos(\theta_w)] \alpha \quad (6)$$

$$265 \quad K_u^B = D_u^B \alpha \approx [1.04(1 + 5.4u)^{0.5}] \alpha \quad (7)$$

266 where θ_w is the subsurface solar zenith angle, α is defined as $(a + b_b)$, and u is defined as
 267 $b_b/(a + b_b)$. If we treat the bottom of the water as the Secchi disk, and assume that the disk is a
 268 lambertian object, then the second term on the right side of Eq. (5) becomes the light that comes
 269 from the Secchi disk. Therefore, the K_u^B can be considered to be the K_T in the new Z_{SD} theory
 270 (i.e., $K_T = K_u^B$). By converting the subsurface solar zenith angle θ_w to the above surface solar
 271 zenith angle θ , and combining the Eqs. (6) and (7), the ratio of K_T and K_d can be expressed as:

$$272 \quad K_T/K_d = \frac{1.04(1+5.4u)^{0.5}}{1/\left(1-\frac{\sin(\theta)^2}{RI^2}\right)^{0.5}} \quad (8)$$

273 where RI is the refractive index value of the water (1.34, Lee et al., 1998). By replacing the fixed
 274 value of 2.5 in Eq. (3) with $(1+K_T/K_d)$, the Lee15 algorithm can be modified as:

$$275 \quad Z_{SD} = \frac{1}{(1+K_T/K_d) \cdot \text{Min}(K_d(\lambda))} \ln \left(\frac{|0.14 - R_{rs}^{PC}|}{c_t^r} \right) \quad (9)$$

276 3.3. Accuracy assessment

277 We used the root mean square error (RMSE), the mean absolute percentage error (MAPE),
 278 and bias to evaluate the performance of the improved Lee15 algorithm. The equations are as

279 follows:

$$280 \quad RMSE = \sqrt{\frac{\sum_{i=1}^N (X_{estimated,i} - X_{measured,i})^2}{N}} \quad (10)$$

$$281 \quad MAPE = \frac{1}{N} \sum_{i=1}^N \left| \frac{X_{estimated,i} - X_{measured,i}}{X_{measured,i}} \right| \cdot 100\% \quad (11)$$

$$282 \quad Bias = \frac{1}{N} \sum_{i=1}^N (X_{estimated,i} - X_{measured,i}) \quad (12)$$

283 where $X_{estimated}$ is the estimated parameter (e.g., a , K_d or Z_{SD}), $X_{measured}$ is the
284 corresponding in situ measurement, and N is the number of data. The determination coefficient
285 (R^2) was also calculated for reference.

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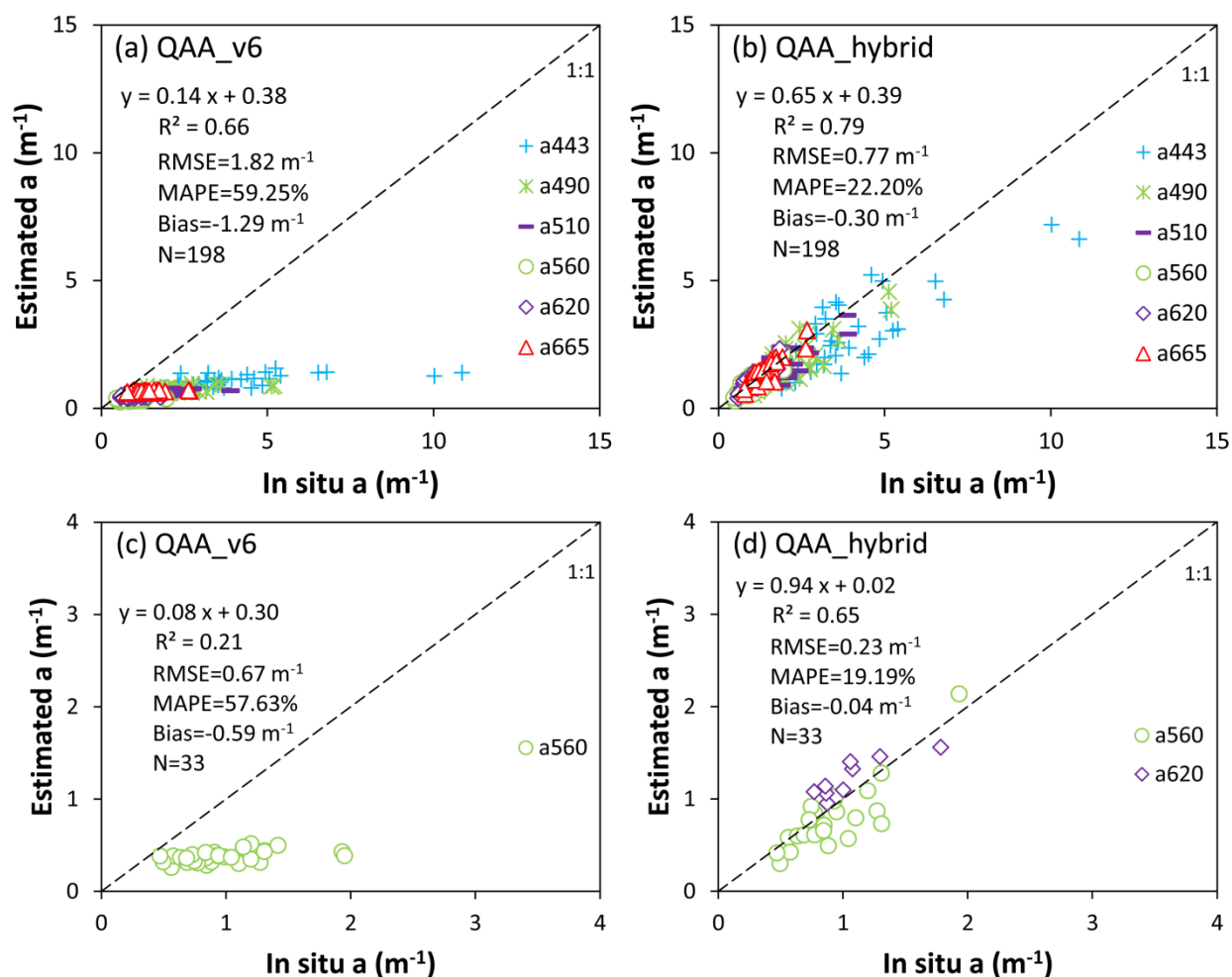
287 4. Results

288 4.1. The a , K_d and Z_{SD} values estimated from in situ R_{rs} spectra

289 Figure 3 shows the results of our comparisons of the derived $a(\lambda)$ and in situ $a(\lambda)$ at all
290 MERIS visible bands. It can be seen that the QAA_v6 gave larger underestimations of $a(\lambda)$ at
291 all visible bands, with $RMSE = 1.82 \text{ m}^{-1}$, $MAPE = 59\%$ and $Bias = -1.29 \text{ m}^{-1}$ (Fig. 3a). In
292 contrast, the QAA_hybrid showed better retrievals of $a(\lambda)$ at all visible bands with
293 $RMSE = 0.77 \text{ m}^{-1}$, $MAPE = 22\%$ and $Bias = -0.30 \text{ m}^{-1}$ (Fig. 3b). The determination coefficient
294 was also increased from 0.66 to 0.79. However, some retrieved absorption coefficients at 443 nm
295 (data collected from Lake Kasumigaura on April 18, 2016) still showed slight underestimations.

296 We checked the bands corresponding to the minimum K_d and found that 443 nm was not

297 selected for Z_{SD} estimations. If we compare only the retrieved $a(\lambda)$ and the in situ $a(\lambda)$ at the
 298 selected bands (i.e., the band with minimum K_d in visible domain and finally used for Z_{SD}
 299 estimations), no obvious underestimations or overestimations from the use of QAA_hybrid were
 300 observed (Fig. 3d), whereas the QAA_v6 still showed larger underestimated $a(\lambda)$ at the
 301 selected bands (Fig. 3c). The values of RMSE, MAPE, Bias, and R^2 were calculated as 0.23 m^{-1} ,
 302 19%, -0.04 m^{-1} , and 0.65, respectively, with the use of the QAA_hybrid at the selected bands.

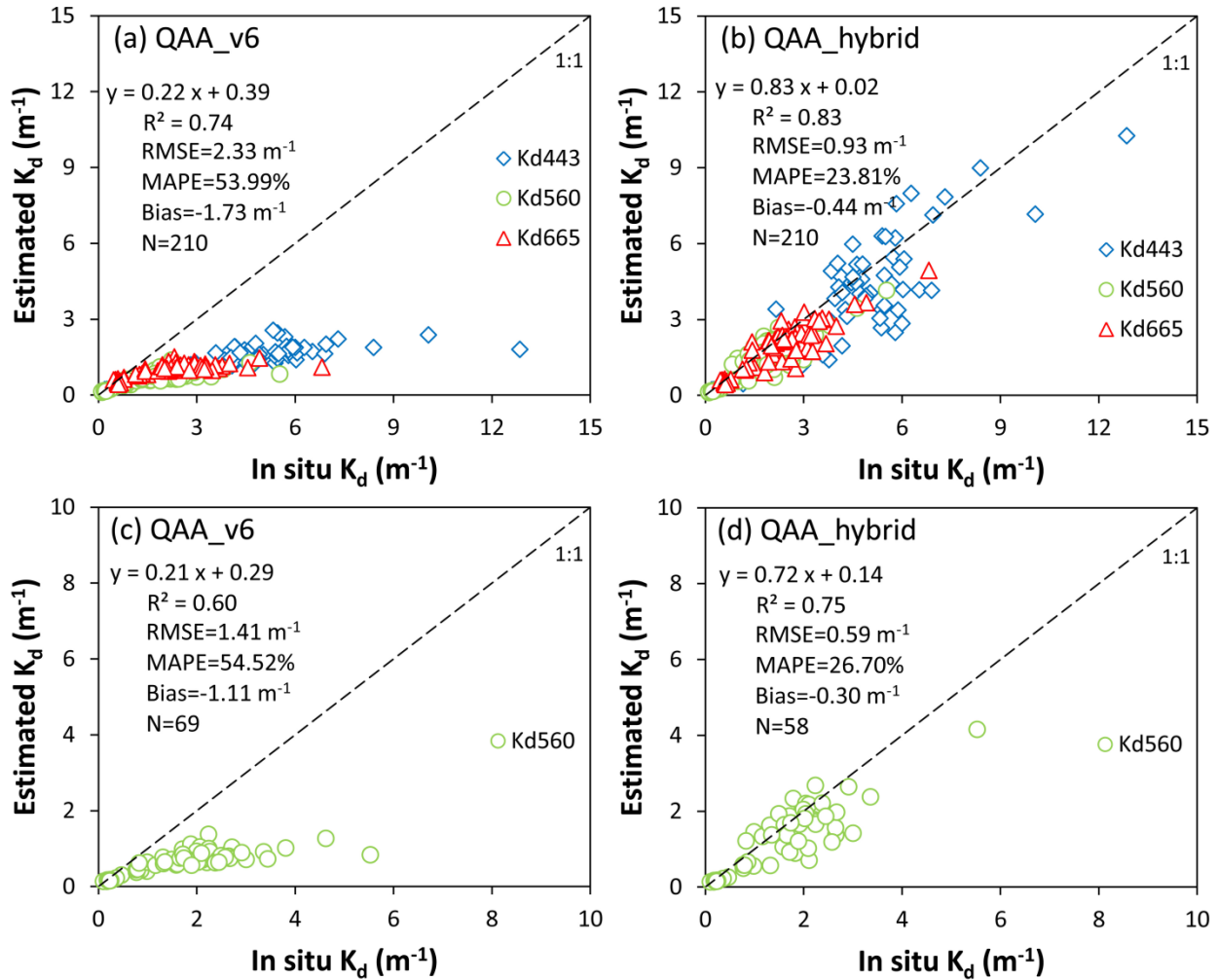


303
 304 **Fig. 3.** Comparison between in situ absorption coefficients and estimated absorption coefficients,

305 estimated using (a) QAA_v6 at all MERIS visible bands, (b) QAA_hybrid at all MERIS visible
306 bands, (c) QAA_v6 only at the bands corresponding to the minimum K_d values, and (d) the
307 QAA_hybrid only at the bands corresponding to the minimum K_d values.

308

309 Figure 4 illustrates the results of our comparisons of the retrieved K_d and the in
310 situ-measured K_d at 443, 555 and 669 nm. It can be seen that using $a(\lambda)$ and $b_b(\lambda)$ estimated
311 from the QAA_v6 resulted in large underestimations of K_d (RMSE = 2.33 m⁻¹, MAPE = 54% and
312 Bias = -1.73 m⁻¹, Fig. 4a), and these underestimations were largely improved by using the
313 QAA_hybrid instead of QAA_v6 (RMSE = 0.93 m⁻¹, MAPE = 24% and Bias = -0.44m⁻¹, Fig.
314 4b). We also compared only the K_d at the bands finally used for the Z_{SD} estimations (i.e., the
315 minimum K_d) and the corresponding in situ-measured K_d ; similar improvements were found by
316 comparing the use of $a(\lambda)$ and $b_b(\lambda)$ obtained from QAA_v6 with those obtained using the
317 QAA_hybrid (Fig. 4c, d). It should be noted that the smaller numbers of data in Fig. 4c and Fig.
318 4d are because the estimated minimum K_d values were found at wavelengths without in situ
319 measurements for some sampling sites.



320

321 **Fig.4.** Comparison between in situ-measured K_d and estimated K_d at bands of 443 nm, 560 nm

322 and 665 nm. (a) Estimated $K_d(\lambda)$ using $a(\lambda)$ and $b_b(\lambda)$ from QAA_v6. (b) Estimated $K_d(\lambda)$

323 using $a(\lambda)$ and $b_b(\lambda)$ from the QAA_hybrid. (c) Only the estimated K_d at the minimum K_d

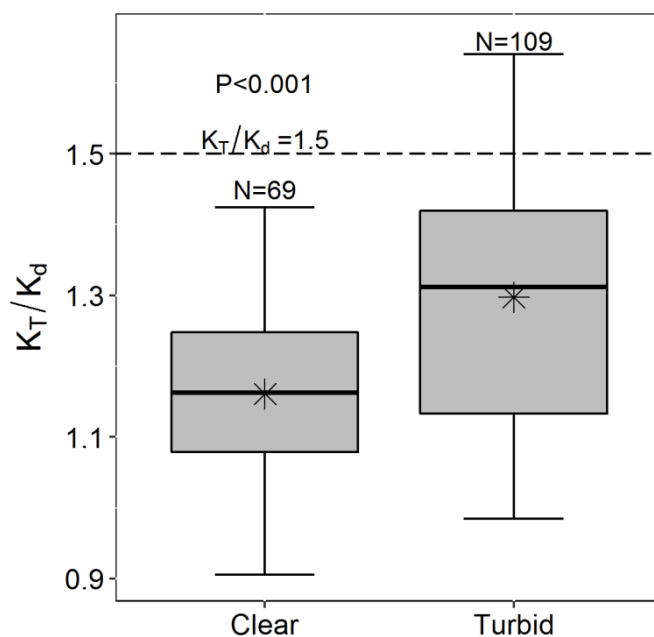
324 bands using $a(\lambda)$ and $b_b(\lambda)$ from QAA_v6. (d) Only the estimated K_d at the minimum K_d

325 bands using $a(\lambda)$ and $b_b(\lambda)$ from the QAA_hybrid.

326

327 Figure 5 shows the estimated K_T/K_d ratios obtained using Eq. (8) for all available data

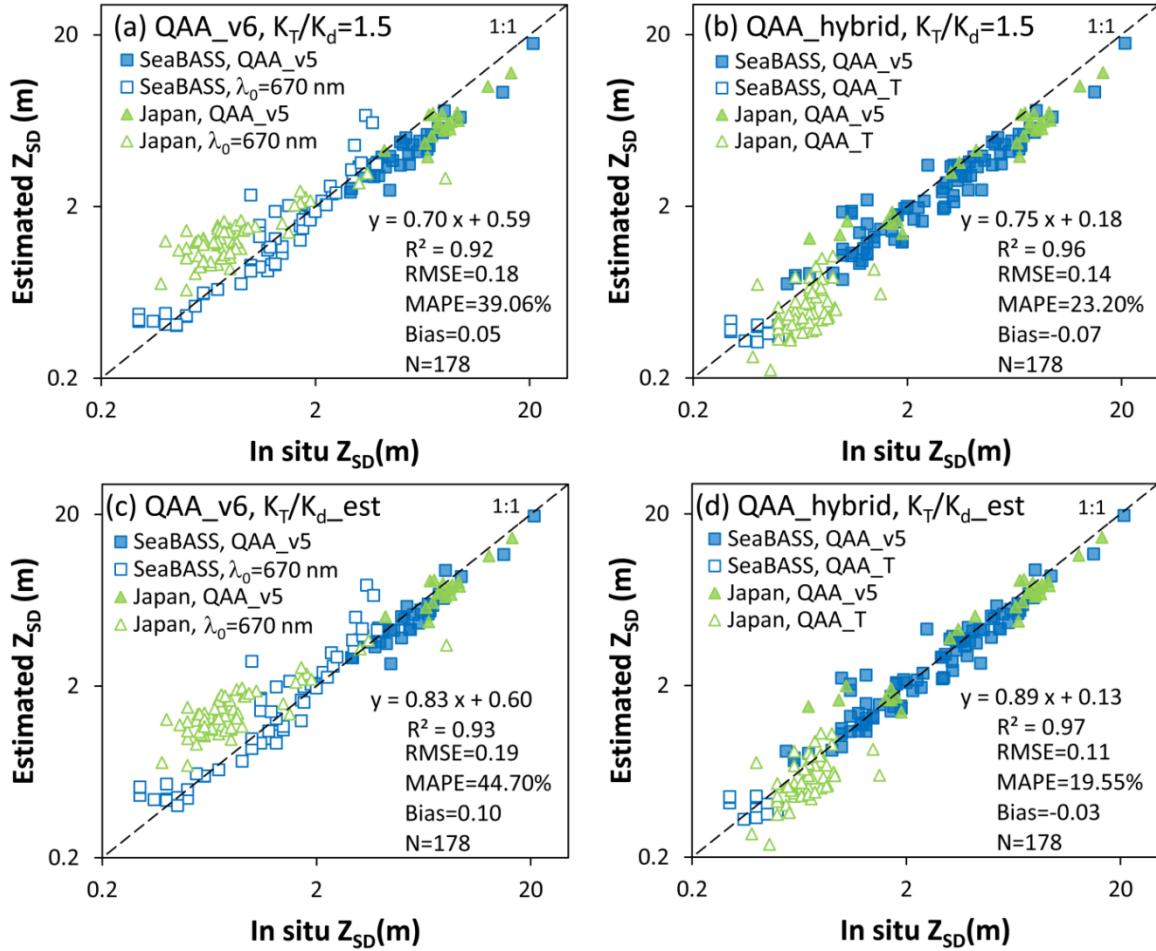
328 (N=178). The results showed that the K_T/K_d ratios ranged from 0.91 to 1.64 with an average
 329 value of 1.24. These ratios were different from the fixed value of 1.5 used in the original Lee15
 330 algorithm. In addition, the K_T/K_d ratios of clear waters (i.e., Z_{SD} values ≥ 2 m) were
 331 significantly lower than those of turbid waters (i.e., Z_{SD} values < 2 m), with a mean K_T/K_d ratio
 332 of 1.16 in clear waters and 1.30 in turbid waters ($P < 0.001$).



333
 334 **Fig. 5.** Comparison of estimated K_T/K_d values between clear (Z_{SD} values ≥ 2 m) and turbid (Z_{SD}
 335 values < 2 m) waters. *Black star:* The mean K_T/K_d ratio. *Dashed line:* $K_T/K_d = 1.5$, which
 336 was used in the original Lee15 algorithm.

337
 338 Figure 6 shows the results of our comparisons of the estimated and in situ-measured Z_{SD}
 339 values. The results showed that: (1) the original Lee15 algorithm clearly underestimated the Z_{SD}

340 in clear waters (solid symbols) and overestimated the Z_{SD} in turbid waters (hollow symbols),
341 with the RMSE of 0.18 in log10 unit and MAPE of 39% (Fig. 6a); (2) the overestimations in
342 turbid waters were improved by using the QAA_hybrid instead of QAA_v6, with a reduced
343 RMSE of 0.14 in log10 unit and MAPE of 23% (Fig. 6b; hollow symbols); (3) the
344 underestimations in clear waters were much improved by using dynamic K_T/K_d ratios instead
345 of the constant ratio of 1.5, even with slightly increased RMSE of 0.19 in log10 unit and MAPE
346 of 45% (Fig. 6c; solid symbols); and (4) both overestimations and underestimations were
347 improved by combining the QAA_hybrid and dynamic K_T/K_d ratios, with a reduced RMSE of
348 0.11 in log10 unit and MAPE of 20% (Fig. 6d). The slope and intercept values of the regression
349 lines were also changed from 0.70 to 0.89 and from 0.59 to 0.13, respectively.



350

351 **Fig. 6.** Comparisons between in situ measured Z_{SD} values and estimated Z_{SD} values from in situ

352 R_{rs} . (a) Estimated Z_{SD} based on QAA_v6 with $K_T/K_d = 1.5$ (i.e., original Lee15 algorithm).

353 (b) Estimated Z_{SD} based on the QAA_hybrid but still with $K_T/K_d = 1.5$. (c) Estimated Z_{SD}

354 based on QAA_v6 but with dynamic K_T/K_d ratios (K_T/K_{d_est}). (d) Estimated Z_{SD} based on

355 the QAA_hybrid with dynamic K_T/K_d ratios (i.e., the improved Lee15 algorithm). Solid

356 symbols represent the Z_{SD} estimated using 560 nm as reference band in both QAA_v6 and

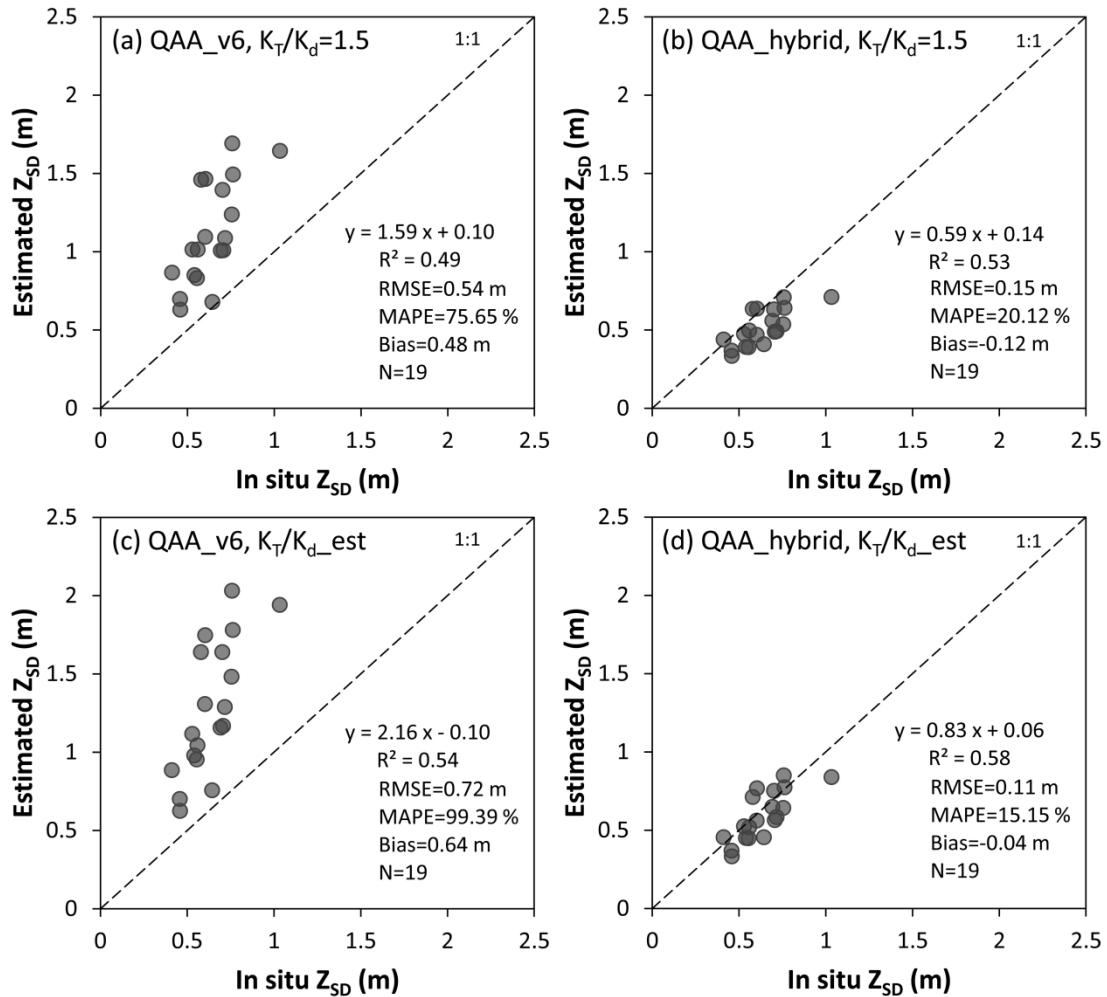
357 QAA_hybrid (i.e., QAA_v5), and hollow symbols represent the Z_{SD} estimated using 670 nm as

358 reference band in QAA_v6 and using 754 nm as reference band in QAA_hybrid (i.e., QAA_T).

359

360 4.2. Z_{SD} estimated from MERIS data in Lake Kasumigaura

361 Figure 7 shows the comparisons of the estimated Z_{SD} values from actual MERIS data and
362 the in situ-measured Z_{SD} values for 19 matchups (with time windows ≤ 4 hours and differences
363 of solar zenith angles ≤ 9 degree). Similar to the results showed in Figure 6, the improved Lee15
364 algorithm achieved the best performance with the smallest RMSE of 0.11 m, MAPE of 15%, and
365 the highest determination coefficient of 0.58 (Fig. 7d). The original Lee15 algorithm
366 overestimated the Z_{SD} in Lake Kasumigaura (Fig. 7a). These overestimations were improved
367 mainly by using the QAA_hybrid instead of QAA_v6 (Fig. 7b, with the RMSE reduced from
368 0.54 m to 0.15 m and the MAPE reduced from 76% to 20%). Figure 7c shows that only using the
369 dynamic K_T/K_d ratios instead of the constant ratio of 1.5 resulted in decreased estimation
370 accuracy with the largest RMSE (0.72 m) and MAPE (99%) values, but improved determination
371 coefficient (from 0.49 to 0.54).



372

373 **Fig. 7.** Comparisons of the in situ Z_{SD} and estimated Z_{SD} values from MERIS data. (a) Estimated

374 Z_{SD} using QAA_v6 with $K_T/K_d = 1.5$ (i.e., the original Lee15 algorithm). (b) Estimated Z_{SD}

375 using the QAA_hybrid but still with $K_T/K_d = 1.5$. (c) estimated Z_{SD} using QAA_v6 but with

376 dynamic K_T/K_d ratios (K_T/K_{d_est}). (d) Estimated Z_{SD} using the QAA_hybrid with dynamic

377 K_T/K_d ratios (i.e., the improved Lee15 algorithm).

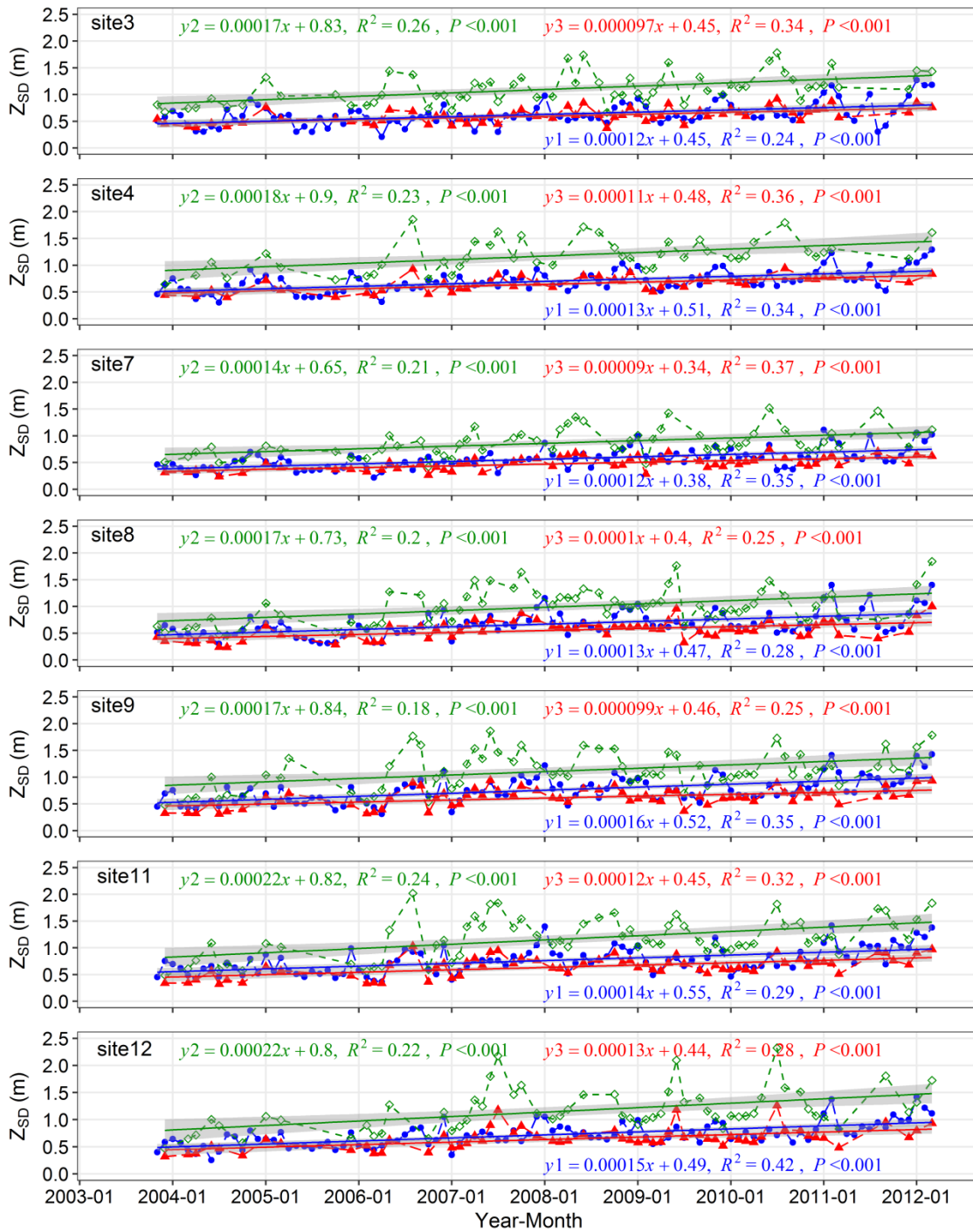
378

379 Figure 8 shows the comparisons of the monthly measured and estimated Z_{SD} values in

380 Lake Kasumigaura for a long-term period (2003–2012). The monthly measured Z_{SD} values were
381 obtained from the NIES-dataset, and the monthly estimated Z_{SD} values were obtained from the
382 available MERIS data between 2003 and 2012 using the **original Lee algorithm** and the improved
383 Lee15 algorithm. Sites 1, 2 and 6 of Lake Kasumigaura were excluded from the comparison
384 because they are too close to the shoreline and strongly influenced by the land (i.e. no any
385 available estimated Z_{SD} values within the 3×3 windows after one pixel buffer from shoreline was
386 removed). In total, we obtained 200 MERIS images; however, because a few sites were covered
387 by clouds, cloud shadows, or not covered by MERIS images (Lake Kasumigaura was partly
388 covered by one MERIS image), there were the following numbers of available MERIS images
389 for the sites: 122 images for site 3; 72 images for site 4; 114 images for site 7; 135 images for
390 site 8; 138 images for site 9; 133 images for site 11; and 124 images for site 12.

391 Overall, the temporal trends of Z_{SD} values obtained from MERIS data by using the
392 improved Lee15 algorithm (**red line with triangles**) agreed well with those obtained from field
393 surveys (**blue line with circles**) at all seven sites. Both the monthly estimated Z_{SD} values **using**
394 **the improved Lee15 algorithm** and the monthly in situ-measured Z_{SD} values showed a significant
395 increase trend in Lake Kasumigaura during the 10-year study period (with all slopes > 0 and all P
396 values < 0.001). **In contrast, the estimated Z_{SD} using the original Lee15 algorithm showed**
397 **obvious overestimations and lower R^2 values in the temporal trend analyses (green line with**

398 diamonds).



399

400 **Fig. 8.** Monthly Z_{SD} changes from 2003 to 2012 at seven sites in Lake Kasumigaura. Blue

401 dashed line with solid circles represents monthly in situ-measured Z_{SD} values, and blue solid line

402 represents temporal trend obtained from the monthly in situ-measured Z_{SD} values (y1); red
403 dashed line with solid triangles represents monthly mean MERIS-derived Z_{SD} values using the
404 improved Lee15 algorithm, and red solid line represents temporal trend obtained from the
405 monthly mean MERIS-derived Z_{SD} values using the improved Lee15 algorithm (y3); green
406 dashed line with hollow diamonds represents monthly mean MERIS-derived Z_{SD} values using
407 the original Lee15 algorithm, and green solid line represents temporal trend obtained from the
408 monthly mean MERIS-derived Z_{SD} values using the original Lee15 algorithm (y2).

409

410 5. Discussion

411 5.1. Necessity of the QAA_hybrid

412 The estimations of $a(\lambda)$ and $b_b(\lambda)$ using QAA_v6 is the first step in the original Lee15
413 algorithm (Lee et al., 2015a). Both previous studies and our results have confirmed that the
414 estimation errors that occur in this step will be propagated to the $K_d(\lambda)$ estimations in the second
415 step and then the Z_{SD} estimations in the final step (Yang et al., 2014, 2015; Figs. 3a, 4a, and 6a in
416 this study). Failures of QAA_v6 applications usually occurred in turbid waters (Yang et al.,
417 2014; Wang et al., 2017; Rodrigues et al., 2017). It is thus necessary to use an alternative to
418 QAA_v6 for turbid waters.

419 Although several modified QAAs have been proposed for retrieving $a(\lambda)$ and $b_b(\lambda)$

420 values in turbid waters, two empirical relationships for estimating the absorption coefficient at a
421 reference band ($a(\lambda_0)$, step 4 in Table 2) and the spectral slope of the backscattering coefficient
422 of suspended particles (Y , step 6 in Table 2) must be recalibrated by using in situ data in most of
423 these modified QAAs (Le et al., 2009; Huang et al., 2014; Mishra et al., 2014; Wang et al., 2017).
424 The constant requirement of in situ data for model recalibration will make the two empirical
425 relationships the first important equations in these modified QAAs, and thus will limit their
426 applicability in various waters. In contrast, QAA_T proposed by Yang et al. (2013) does not
427 include empirical equations for $a(\lambda)$ and $b_b(\lambda)$ retrievals, and thus it is the most proper
428 algorithm to replace QAA_v6 for retrieving $a(\lambda)$ and $b_b(\lambda)$ in turbid waters (Yang et al., 2014,
429 2015; Fukushima et al., 2016).

430 However, QAA_T did not work well in clear waters. For example, if we used QAA_T to
431 retrieve $a(\lambda)$ and $b_b(\lambda)$ for waters with an in situ $Z_{SD} \geq 2$ m (there are 69 such points in Fig.
432 6), larger errors occurred in the estimated Z_{SD} values with the RMSE of 5.24 m, the MAPE of
433 77%, and the very low determination coefficient of 0.01 (data not shown). In contrast, QAA_v5
434 performed very well for these points with the RMSE of 1.01 m, the MAPE of 14%, and the
435 determination coefficient of 0.94.

436 In QAA_hybrid, we selected QAA_v5 for clear waters rather than QAA_v6. This is
437 because that we found QAA_v5 outperformed QAA_v6 in our dataset. Figure 9 shows the

438 comparison of the estimated Z_{SD} values using QAA_v5 and using QAA_v6 for 59 R_{rs} spectra.

439 The 59 R_{rs} spectra were selected by using the criteria of $MCI \leq 0.0016 \text{ sr}^{-1}$ and $R_{rs}(670) > 0.0015$

440 sr^{-1} . In other words, the 59 R_{rs} spectra would select 670 nm as reference band if we used

441 QAA_v6 instead of QAA_v5 for clear waters. In contrast, all R_{rs} spectra with $MCI \leq 0.0016 \text{ sr}^{-1}$

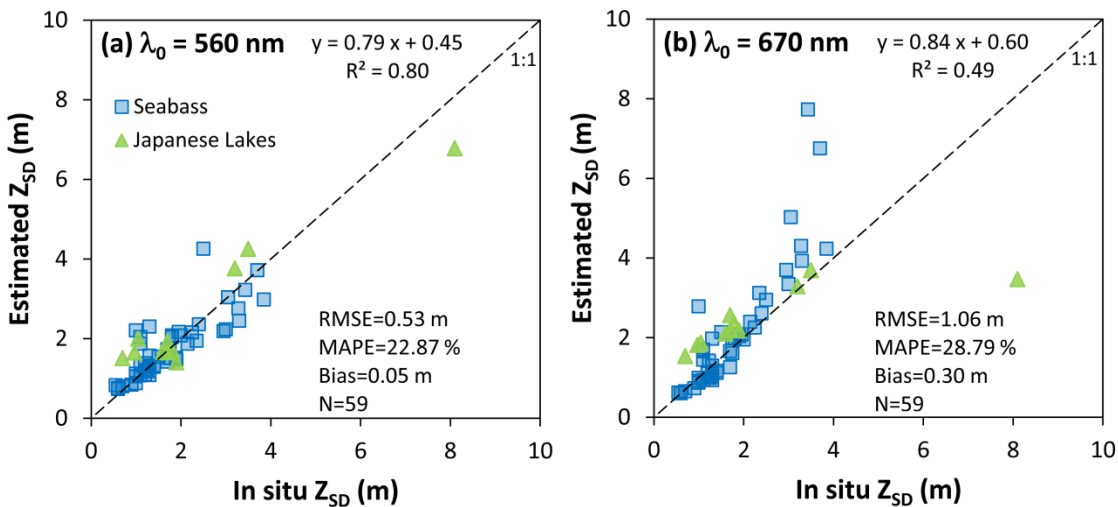
442 (111 R_{rs} spectra in total) only used 560 nm as reference band in QAA_hybrid. From Figure 9, it

443 can be seen that QAA_v5 (left) performed better than QAA_v6 (right) with the RMSE reduced

444 from 1.06 m to 0.53 m, the MAPE reduced from 29% to 23%, and the R^2 increased from 0.49 to

445 0.80. The above findings indicate that it is necessary to select the appropriate QAA according to

446 water turbidities. In other words, it is necessary to use a hybrid QAA to address various waters.



447

448 **Fig. 9.** Comparisons between in situ-measured Z_{SD} values and corresponding estimated Z_{SD}

449 values from 59 selected in situ R_{rs} (see text for details). (a) using 560 nm as reference band; (b)

450 using 670 nm as reference band.

451

452 In this study, we used $MCI = 0.0016 \text{ sr}^{-1}$ to switch QAA_v5 and QAA_T. This MCI
453 threshold was suggested by Matsushita et al. (2015) based on the data collected from five Asian
454 lakes (Lake Erhai and Lake Dianchi in China; Lake Biwa, Lake Suwa, and Lake Kasumigaura in
455 Japan). Our present findings also demonstrated that this threshold is reasonable. Other
456 information can also be used to select the appropriate QAA. For example, Moore et al. (2014)
457 proposed a method to classify waters into seven optical water types (OWTs); Spyrakos et al.
458 (2018) identified 13 OWTs for inland waters based on comprehensive data from more than 250
459 aquatic systems. Further study is needed to compare the performances of different water
460 classification algorithms for selecting the most appropriate QAAs.

461 5.2. The importance of the estimation of the K_T/K_d ratio

462 The reported K_T/K_d ratios range from 0.5 to 2.0 (Philpot, 1989; Maritorena et al., 1994;
463 Lee et al., 1994). In the present study, the K_T/K_d ratios were estimated in the range of 0.91–1.64
464 with an average of 1.24 (Fig. 5). This range is similar to that reported by Maritorena et al. (1994)
465 with K_T/K_d ratios between 1.02 and 1.66. Our results also showed that the K_T/K_d ratios in clear
466 waters are significantly smaller than those in turbid waters (Fig. 5, $p < 0.001$). This finding agrees
467 with Philpot (1989), who reported that the K_T/K_d ratios tended to be higher in strongly absorbing
468 waters.

469 Compared to the K_T/K_d ratios in turbid waters (with a mean ratio of 1.30), the K_T/K_d ratios
470 in clear waters (with a mean ratio of 1.16) are far smaller than the constant K_T/K_d ratio of 1.5
471 used in the original Lee15 algorithm. The above findings indicate that the use of the constant
472 K_T/K_d ratio of 1.5 will lead to larger underestimations of the Z_{SD} in clear waters. For example, in
473 Lake Motosu, a clear Japanese lake with the in situ-measured Z_{SD} of 16.4 m, the K_T/K_d ratio was
474 estimated to be 1.06 by using Eq. (8); the estimated Z_{SD} using the original Lee15 algorithm was
475 12.01 m with a relative error of 26.8% (Fig. 6a), and this error was reduced to 11.2% by using
476 the improved Lee15 algorithm (the estimated $Z_{SD} = 14.58$ m, Fig. 6d). Even in a turbid Japanese
477 lake, i.e., Lake Kasumigaura, the use of dynamic K_T/K_d ratios also improved the Z_{SD} estimations
478 (Fig. 7b vs. Fig. 7d).

479 Although our results have confirmed that the use of the dynamic K_T/K_d ratios can improve
480 Z_{SD} estimations in both clear and turbid waters, further study is still needed to evaluate the
481 relationship between K_T and K_d in various waters due to the Eq. (8) is based on an assumption of
482 treating a Secchi disk as a lambertian bottom.

483 5.3. Applicability of the improved Lee15 algorithm

484 Similar to the original Lee15 algorithm, the improved Lee15 algorithm does not require
485 any in situ data for recalibration. This is because both the QAA_hybrid (the combination of
486 QAA_v5 and QAA_T) and the equation for estimating K_T/K_d ratios (i.e., Eq. (8)) are designed as

487 only using semi-analytical equations, which indicates that the assumptions and empirical
488 equations are all of secondary importance for Z_{SD} retrievals (Lee et al., 1998, 2002, 2015a; Yang
489 et al., 2013). Therefore, although we validated the improved Lee15 algorithm by using only the
490 data collected from 8 Japanese lakes and SeaBASS dataset, it is apparent that the algorithm can
491 also be applied for Z_{SD} estimations in other waters worldwide.

492 Since both the original and improved Lee15 algorithms used only a single band for Z_{SD}
493 retrieval (i.e., the band with the minimum K_d), an accurate algorithm for atmospheric correction
494 is crucial when actual satellite data are used. For clear waters, the atmospheric correction
495 algorithm proposed by Gordon and Wang (1994) will be the best choice, whereas for turbid
496 waters, although there are several algorithms (e.g., Ruddick et al., 2000; Wang and Shi, 2007;
497 Guanter et al., 2007; Doerffer and Schiller, 2008; Bailey et al., 2010; Jaelani et al., 2015), it is
498 still not clear which is the most appropriate algorithm for atmospheric correction. Our present
499 results showed that the Case-2 Regional Processor proposed by Doerffer and Schiller (2008) can
500 be an option for turbid inland waters such as Lake Kasumigaura (Fig. 7). Further validations
501 obtained by using more comprehensive datasets should be carried out in the future to further
502 confirm the above considerations.

503

504 **6. Conclusions**

505 The original Lee15 algorithm showed overestimations of Z_{SD} values in turbid waters and
506 underestimations of Z_{SD} values in clear waters. In the present study, the use of QAA_hybrid
507 instead of QAA_v6 mainly overcame the former shortcoming through blending QAA_T and
508 QAA_v5 for estimating more accurate absorption and backscattering coefficients in both turbid
509 (QAA_T) and clear waters (QAA_v5); and the use of the dynamic K_T/K_d ratios instead of using
510 the fixed K_T/K_d ratio (i.e., 1.5) mainly overcame the latter shortcoming in the original Lee15
511 algorithm. Our results show that the improved Lee15 algorithm gave more accurate Z_{SD}
512 estimations, with RMSE reduced from 0.18 to 0.11 (in log10 unit) and MAPE reduced from 39%
513 to 20% for using the in situ R_{rs} values from 8 Japanese lakes (Z_{SD} values ranged from 0.4 m to
514 16.4 m, N=84) and SeaBASS dataset (Z_{SD} values ranged from 0.3 m to 20.8 m, N=94). The
515 improved Lee15 algorithm is expected to estimate more accurate Z_{SD} values in various types of
516 waters.

517

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525

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