# Outrigger tuned inertial mass electromagnetic transducers for high-rise buildings subject to long period earthquakes

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# Abstract

This paper proposes outrigger tuned inertial mass electromagnetic transducer (TIMET) systems for high-rise buildings subject to long period earthquake excitations. The proposed outrigger TIMET systems consist of the outrigger and TIMET parts. The outrigger damping systems have been proposed as a novel energy dissipation approach to high-rise buildings, in which control devices are installed vertically between the outrigger and perimeter columns to achieve large energy dissipation. While the TIMET has been developed based on the mechanism of the tuned viscous mass damper (TVMD) which can improve energy absorbing capability by taking advantage of resonance effect. However, instead of a viscous material, the damping of the TIMET is provided by a motor which can convert mechanical energy to electrical energy. The focus of this study is to investigate the structural control performance and energy harvesting efficiency of the proposed outrigger TIMET system for high-rise buildings subjected to long period earthquakes through numerical simulations.

*Keywords:* Outrigger damping system, Tuned inertial mass electromagnetic transducer, Energy harvesting, High-rise building, Long period earthquake

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#### 1. Introduction

As new materials and technologies have been developed, the number of highrise buildings has been rapidly increasing especially in urban areas all over the world. However, at the same time this achievement brings new problems regarding protection of these buildings against strong winds and severe earthquakes. In particular, because high-rise buildings have dominant natural frequencies in low frequency range, the vulnerability to long period earthquakes has been pointed out. Therefore structural control strategies targeting the specified frequency range is demanding for protecting high-rise buildings.

Traditionally, a tuned mass damper (TMD) [1] has been employed to accomplish this objective. However, due to the restricted auxiliary mass for practical reasons, the effectiveness of the TMD systems to earthquake ground motions is limited [2]. To address this issue, recently, for the purpose of the seismic response reduction of civil structures, various types of control devices utilizing a tuned inerter has been developed by many researchers, including the tuned viscous mass damper (TVMD) [3], tuned inerter damper (TID) [4, 5], tuned mass damper inerter (TMDI) [6], and T tuned inerter damper (TTID) [7]. As explained in [8] originally, the amplified equivalent mass effect, i.e., *inertance*, is realized by a mechanism such as the hydraulic [9], ball screw [3], or rack and pinion inerter [8, 10] and the force proportional to the relative acceleration between both ends is produced.

For example, the TVMD proposed in [3] consists of two parts: a rotational mass damper and a tuning spring. Moreover, the rotational mass damper part can be divided into a ball screw mechanism, a rotating mass, and a viscous damper. The ball screw mechanism is employed to convert translational motion to rotational behavior. Then by rotating the relatively small physical mass, an amplified equivalent mass effect, i.e., inertance, is obtained. The device producing up to on the order of thousandfold equivalent mass has been already developed [11]. This makes it possible for the TVMD to realize large mass ratio to the structure enough that a typical TMD can not realize. And the input energy is absorbed by the viscous material as heat. In this system, the inertance and the viscous damper are connected in parallel and the tuning spring is arranged in series with them. Then the TVMD is connected to the structure through the spring. Thus the energy absorption efficiency and vibration mitigation performance can be improved by tuning the spring stiffness so that the rotational inertial mass resonates with the structure [3].

Based on the mechanism of the TVMD, the first author proposed a tuned inertial mass electromagnetic transducer (TIMET) [12], in which a motor is employed instead of a viscous material to convert mechanical energy into electrical energy. And the effectiveness of the TIMET on the civil structures subjected to earthquake loadings was verified using the small-scale three story benchmark building model through numerical simulation studies [13]. During seismic events, an external power source is not guaranteed, so the generated energy by the motor is of value to self-powered control, structural health monitoring, emergency power supply and so on. Similar energy harvesting devices employing

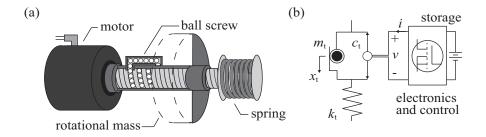


Figure 1: TIMET: (a) Schematic illustration, (b) Model

the tuned inerter mechanism for civil structures have been proposed by other researchers [14, 15].

In this research, to take full advantage of the TIMET on high-rise buildings, the outrigger damping system [16, 17, 18] is combined with the TIMET. The outrigger damping system employs damping devices installed between outrigger walls and perimeter columns in a frame-core-tube structure to enhance structural dynamic performance. This paper seeks to verify the efficacy of the outrigger TIMETs for high-rise buildings subject to long period earthquakes. First the mechanism of the TIMET is reviewed briefly. Then the equation of motion of the outrigger TIMET system is developed and the parameter design method is introduced. Numerical simulation studies are carried out by using long period earthquakes and the vibration reduction performance and energy harvesting capability are investigated. Finally, conclusions obtained from this research follow.

# 2. Tuned inertial mass electromagnetic transducer

In this section, the mechanism and model of the TIMET is overviewed. Also the definition of generated energy used in this paper is derived.

#### 2.1. Model

The TIMET employed in this research is illustrated schematically in Figure 1(a) and its model is shown in Figure 1(b). As can be seen, the TIMET consists of three parts: a motor, a ball screw mechanism with a rotational mass, and a turning spring. The TIMET provides damping by the motor to decay vibration and vibration energy is converted into electrical energy. In this paper, the damping coefficient provided by the motor is denoted by  $c_t$ . In parallel with the motor, inertance  $m_t$ , which is realized through a ball screw mechanism, is installed. And the linear spring whose stiffness is  $k_t$  is installed in series with the motor and inertance. To improve energy absorbing efficiency and vibration mitigation performance, we need to design the value of  $k_t$  and  $c_t$  appropriately.

The damping  $c_t$  can be decided by controlling the current into the motor *i*. The relationship between the current and voltage is defined as

$$i = -Yv \tag{1}$$

where Y is a time-invariant feedback gain, which can be adjusted by a transistor such as a MOSFET. Under this feedback law, the electrical load can be considered a resistor. Thus Y has units of admittance. And the voltage v can be expressed, through the back-EMF constant  $e_t$ , as

$$v = e_t \dot{x}_t \tag{2}$$

where  $x_t$  is the displacement of the inertance  $m_t$ . Let the electromechanical transduction power be  $P_e$  and the damping force by the motor be  $f_c$ . Since the electromechanical transduction power is preserved between mechanical and electrical sides of the transducers,

$$P_e = iv = f_c \dot{x}_t \tag{3}$$

with the convention that positive  $P_e(t)$  implies energy flow from the electrical network to the mechanical system. Under this definition, the damping force by the motor is given by

$$f_c = -c_t \dot{x}_t \tag{4}$$

Thus from Eqs. (1), (2), and (3), we have

$$-Ye_t^2 \dot{x}_t^2 = -c_t \dot{x}_t^2 \tag{5}$$

Hence the damping  $c_t$  can be expressed as

$$c_t = Y e_t^2 \tag{6}$$

Therefore, we know that the desired damping can be obtained by choosing appropriate Y. Thus, hereafter  $m_t$ ,  $k_t$ , and  $c_t$  are used as design parameter for the TIMET.

### 2.2. Energy harvesting objective

To assess the energy harvesting efficiency for the proposed system, the power delivered to storage needs to be defined. As in [19, 20], the power delivered to storage  $P_g$  is defined as the power extracted by the transducer minus the transmission losses in the transducer and power electronic circuitry  $P_l$ , i.e.,

$$P_q(t) = -P_e(t) - P_l(t) \tag{7}$$

Typically the expression for the transmission losses  $P_l(t)$  is quite complicated because the transmission losses happen due to various causes on the electronic hardware. However, for the purpose of this paper, we assume simply that the transmission loss is resistive; i.e.,

$$P_l(t) = i^2 R = \frac{c_t^2 R}{e_t^2} \dot{x}_t^2$$
(8)

where R > 0 is the transmission resistance. For example, if the losses were entirely comprised of coil losses in the transducers, then R is equal to the coil resistance. For more complex loss models, which incorporate MOSFET and diode conduction losses in the converters, past work has shown that these situations can also be conservatively approximated by a resistive loss term, together with a static power offset [21]. Defining  $\bar{c}_t = e_t^2/R$ , which is a positive value with units of viscous damping, gives

$$P_l(t) = \frac{c_t^2}{\bar{c}_t} \dot{x}_t^2 \tag{9}$$

and physically  $\bar{c}_t$  represents the supplemental viscous damping that would relate the velocity  $\dot{x}_t$  to the output force  $c_t \dot{x}_t$  if the coil of the transducer is shorted. Thus  $\bar{c}_t$  is determined by the specification of the transducer and represents the maximum viscous damping the transducer can exert.

With the above definitions and assumptions, we can now define the power delivered to storage as

$$P_g(t) = \left(c_t - \frac{c_t^2}{\bar{c}_t}\right) \dot{x}_t^2 \tag{10}$$

# 3. Problem formulation

# 3.1. Uncontrolled building

To begin with, the uncontrolled Nth floor building shown in Figure 2(a) is considered. The equation of motion is developed as

$$\mathbf{M}_b \ddot{\mathbf{x}}_b + \mathbf{C}_b \dot{\mathbf{x}}_b + \mathbf{K}_b \mathbf{x}_b = -\mathbf{M}_b \mathbf{\Gamma}_b \ddot{x}_g \tag{11}$$

where  $\mathbf{M}_b$ ,  $\mathbf{C}_b$ , and  $\mathbf{K}_b$  are the structural mass, damping, and stiffness of the uncontrolled building, respectively,  $\mathbf{x}_b$  is the structural deformation vector,  $\mathbf{\Gamma}_b$  is a vector with entries equal to unity for translational DOFs and zero for others, and  $\ddot{x}_g$  is the horizontal ground acceleration. The structural deformation vector  $\mathbf{x}_b$  defined in this study consists of displacements and rotational angles as

$$\mathbf{x}_b = \begin{bmatrix} x_1 & \theta_1 & x_2 & \theta_2 & \dots & x_N & \theta_N \end{bmatrix}^T$$
(12)

where  $x_j$  and  $\theta_j$  are the displacement and rotational angle relative to the ground of the *j*th floor, respectively. Thus the mass matrix  $\mathbf{M}_b$  is defined as

$$\mathbf{M}_b = \operatorname{diag} \begin{vmatrix} m_1 & I_1 & m_2 & I_2 & \dots & m_N & I_N \end{vmatrix}$$
(13)

where  $m_j$  and  $I_j$  are the mass and mass moment inertia of the *j*th floor, respectively. And the influence vector  $\Gamma_b$  is given by

$$\boldsymbol{\Gamma}_b = \begin{bmatrix} 1 & 0 & 1 & 0 & \dots & 1 & 0 \end{bmatrix}^T \tag{14}$$

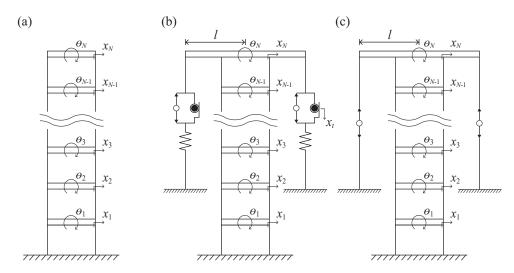


Figure 2: Building models (a) Uncontrolled building, (b) Building with TIMETs, (c) Building with ETs.

# 3.2. Building with outrigger tuned inertial mass electromagnetic transducers

Based on the uncontrolled building case, the equation of motion for the building model with the outrigger TIMETs as illustrated in Figure 2(b) is derived. Let l be the distance from the center of the core to the tips of the TIMET. And considering the 1st mode shape of the building, we assume that the outrigger system is installed on the top floor in this research so that the efficiency of the outrigger TIMETs is maximized. Then the moment applied to the Nth floor from the TIMETs installed on the Nth floor becomes

$$M_{ti,N} = lk_t(l\theta_N - x_t) \tag{15}$$

where  $k_t$  is the stiffness of the supporting spring and  $x_t$  is the relative displacement of the inertial masses of the TIMETs. Let the structural deformation vector be defined as

$$\mathbf{x}_{ti} = \begin{bmatrix} \mathbf{x}_b^T & x_t \end{bmatrix}^T \tag{16}$$

then the equation of motion can be written as

$$\mathbf{M}_{ti}\ddot{\mathbf{x}}_{ti} + \mathbf{C}_{ti}\dot{\mathbf{x}}_{ti} + \mathbf{K}_{ti}\mathbf{x}_{ti} = -\mathbf{M}_{ti}\Gamma_{ti}\ddot{x}_g \tag{17}$$

By taking Eq. (15) and the force equilibrium of the TIMET given by

$$m_t \ddot{x}_t + c_t \dot{x}_t = k_t (l\theta_N - x_t) \tag{18}$$

into account,  $\mathbf{M}_{ti}$ ,  $\mathbf{C}_{ti}$ , and  $\mathbf{K}_{ti}$  matrices can be developed as

$$\mathbf{M}_{ti} = \begin{bmatrix} \mathbf{M}_b & \mathbf{0} \\ \mathbf{0} & m_t \end{bmatrix}, \quad \mathbf{C}_{ti} = \begin{bmatrix} \mathbf{C}_b & \mathbf{0} \\ \mathbf{0} & c_t \end{bmatrix}, \quad \mathbf{K}_{ti} = \begin{bmatrix} \mathbf{K}_{11} & \mathbf{K}_{12} \\ \mathbf{K}_{21} & k_t \end{bmatrix}$$
(19)

where  $m_t$ ,  $k_t$ , and  $c_t$  are the summation of the equivalent mass, tuning spring stiffness, and damping coefficient of the TIMETs connected to the Nth floor, respectively, and

$$\mathbf{K}_{11} = \mathbf{K}_b + \operatorname{diag} \begin{bmatrix} 0 & 0 & \dots & 0 & l^2 k_t \end{bmatrix}, \mathbf{K}_{12} = \begin{bmatrix} 0 & 0 & \dots & 0 & -lk_t \end{bmatrix}^T, \quad \mathbf{K}_{21} = \mathbf{K}_{12}^T$$
(20)

Also, the equivalent mass of the TIMETs are not influenced by horizontal earthquake inputs, so  $\Gamma_{ti}$  is given by

$$\boldsymbol{\Gamma}_{ti} = \begin{bmatrix} \boldsymbol{\Gamma}_b^T & 0 \end{bmatrix}^T \tag{21}$$

#### 3.3. Building with electromagnetic transducers

Finally, to investigate the effect of the tuned inertial mass mechanism, the building model with electromagnetic transducers (ETs) instead of the TIMETs as shown in Figure 2(c) is investigated as well. Let the structural deformation vector be defined as

$$\mathbf{x}_{et} = \mathbf{x}_b \tag{22}$$

Then the equation of motion is derived as

$$\mathbf{M}_{et}\ddot{\mathbf{x}}_{et} + \mathbf{C}_{et}\dot{\mathbf{x}}_{et} + \mathbf{K}_{et}\mathbf{x}_{et} = -\mathbf{M}_{et}\Gamma_{et}\ddot{x}_g \tag{23}$$

where

$$\mathbf{M}_{et} = \mathbf{M}_b, \quad \mathbf{C}_{et} = \mathbf{C}_b + \text{diag} \begin{bmatrix} 0 & 0 & \dots & 0 & l^2 c_t \end{bmatrix}, \quad \mathbf{K}_{et} = \mathbf{K}_b$$
(24)

and

$$\Gamma_{et} = \Gamma_b \tag{25}$$

# 4. Design for outrigger tuned inertial mass electromagnetic transducers

The tuning spring stiffness and damping coefficient by the motor are designed to tune to the 1st mode of the uncontrolled building based on the method introduced in [3] as

$$k_t = (\beta \omega_1)^2 m_t \tag{26}$$

$$c_t = 2\zeta\beta\omega_1 m_t \tag{27}$$

where  $\omega_1$  is the natural frequency of the 1st mode of the uncontrolled building and  $\beta$  is the optimum frequency ratio and  $\zeta$  is the optimum damping coefficient of the 1st mode, which are expressed as

$$\beta = \frac{1 - \sqrt{1 - 4\mu}}{2\mu}, \quad \zeta = \frac{\sqrt{3 - (1 - \sqrt{1 - 4\mu})}}{4} \tag{28}$$

The mass ratio  $\mu$  is defined as

$$\mu = \frac{\boldsymbol{\Phi}^T \mathbf{M}_t \boldsymbol{\Phi}}{\boldsymbol{\Phi}^T \mathbf{M}_b \boldsymbol{\Phi}} \tag{29}$$

where  $\Phi$  is the 1st mode shape vector of the building and  $\mathbf{M}_t$  is defined as

$$\mathbf{M}_t = \operatorname{diag} \begin{bmatrix} 0 & 0 & \dots & 0 & l^2 m_t \end{bmatrix}$$
(30)

This design method is based on the fixed-point theory [1] and aims to reduce the response displacement. The details of this can be found in [3].

#### 5. Numerical simulations

## 5.1. Building model

The building used in this study is the St. Francis Shangri-La Place in Philippines [22, 23, 24]. This 60-story building has a height of 210 m and has 12 perimeter columns which are 20 m from the building center line. The concrete core is assumed to be  $12 \text{ m} \times 12 \text{ m}$  with 0.5 m thickness. The total mass of the building is 30,000 tons and the outrigger system installed consists of 16 viscous dampers, 8 of which control the response in each of the two orthogonal directions. In this study, we consider only one direction and the TIMETs and ETs are employed instead of viscous dampers.

To create the model for evaluation, a vertical cantilever beam model based on the Bernoulli-Euler beam theory is applied. A finite element model is developed so that every story has one translational and one rotational degree of freedoms. Therefore, the total number of degrees-of-freedom should be 120 (60 in translation and 60 in rotation). The first 10 natural frequencies are 0.18, 1.15, 3.14, 6.00, 9.61, 13.84, 18.56, 23.66, 29.06, and 34.66 Hz, respectively. Damping of 2% is assumed in each mode.

The parameters for the outrigger TIMETs used in this article are summarized in Table 1. First the mass ratio defined as Eq. (29) is set as  $\mu = 0.05$ (TIMET (I)) and  $\mu = 0.1$  (TIMET (II)), and the values of the summation of the installed inertance  $m_t$  are derived. Then the summation of the stiffness  $k_t$ , and damping  $c_t$  are calculated based on Eqs. (26) and (27), respectively. The value of  $\bar{c}_t$  depends on the motor and the lead conversion of the ball screw mechanism, thus this value can be determined relatively flexibly. Therefore we assume that  $\bar{c}_t = 10c_t$  for numerical studies. In this study, to show the effect of the tuned inertial mass mechanism, the same values are employed for  $k_t$  and  $c_t$  of the building with the outrigger ETs and numerical simulations are carried out in parallel.

Using the determined parameter values, the transfer functions from input earthquake acceleration to the relative displacement and absolute acceleration of the 60th floor are developed. The magnitudes for the cases of the uncontrolled building and the one with TIMET (II) are depicted in Figure 3. As can be seen, the TIMET mechanism reduces the peak of the 1st mode significantly without

Table 1: Parameters for the outrigger TIMETs

	TIMET(I)	$TIMET(\Pi)$
$\mu$	0.05	0.1
$m_t$ (ton)	87505	175010
$k_t \; (kN/m)$	131693	300158
$c_t \; (kN \; s/m)$	30207	94236

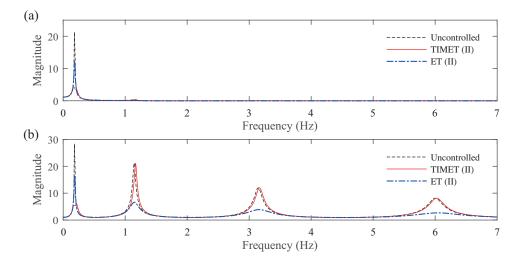


Figure 3: Transfer function from input acceleration to the 60th floor: (a) Displacement, (b) Acceleration.

affecting the higher modes as intended, while the ET case reduces the peaks of the all modes evenly. Also, the figures show that the response accelerations are easily influenced by the higher mode comparing to the response displacements.

# 5.2. Time history analyses

The long period earthquakes used for time history analyses are the EW component of the 2003 Tokachioki earthquake recorded in Tomakomai [25], the 2011 Tohoku earthquake in Osaka [25], and an artificial record assuming the Nankai Trough earthquake in Tokyo area, which is produced by the Building Research Institute, Japan [26]. The time histories of the ground accelerations of these earthquakes are shown in Figure 4.

The results obtained by the numerical simulation studies are shown for the three cases. The peak and root-mean-square (RMS) values of the relative displacements and absolute accelerations of the 20th, 40th, and 60th floors are summarized in Tables 2, 3, and 4. In these table, the peak and RMS values are denoted by p and  $\sigma$ , respectively and the subscripts d or a and digit indicate

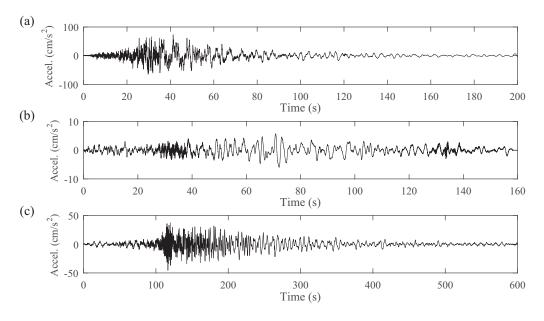


Figure 4: Input earthquakes: (a) Tokachioki, (b) Tohoku, (c) Nankai Trough.

displacement or acceleration and floor number. Also, the averaged generated power  $\bar{P}_q$ , the generated energy defined as

$$E_g = \int_0^{t_f} P_g(t) dt \tag{31}$$

and the input energy during the duration of time 0 to  $t_f$  defined as [27]

$$E_{in} = -\int_0^{t_f} \sum_{j=1}^{60} m_j \ddot{x}_g \dot{x}_{s,j} dt$$
(32)

are summarized in the tables as well as the energy conversion ratio defined as

$$E_r = \frac{E_g}{E_{in}} \times 100 \tag{33}$$

Note that  $t_f$  is 200 s for the Tokachioki, 160 s for the Tohoku, and 600 s for the Nankai Trough earthquake. From these tables, the building with the outrigger TIMET mechanism shows better performance in reducing response displacements and increasing energy absorbing capability to the three earthquake inputs. While the proposed structure does not work well to reduce response accelerations especially to the Nankai Trough earthquake. This is attributed to the fact that the parameters are designed based on the method to reduce the response displacements. Also, this is because the response accelerations are

	Uncontrolled	TIMET (I)	ET(I)	TIMET (II)	ET (II)
$p_{x,20} (cm)$	30.18	22.02	28.62	17.75	25.75
$p_{x,40} ({\rm cm})$	98.32	70.03	93.19	55.96	83.56
$p_{x,60} ({\rm cm})$	180.16	126.42	169.38	101.60	151.86
$\sigma_{x,20} \ (\mathrm{cm})$	9.37	4.71	8.10	3.71	6.48
$\sigma_{x,40} \ (\mathrm{cm})$	30.98	15.42	26.80	12.10	21.44
$\sigma_{x,60} \ (\mathrm{cm})$	56.70	28.02	49.05	21.92	39.23
$p_{a,20} \; ({\rm cm/s^2})$	155.54	151.92	127.59	145.83	103.68
$p_{a,40} \; ({\rm cm/s^2})$	172.72	140.78	150.73	130.14	139.89
$p_{a,60} \; ({\rm cm/s^2})$	322.12	248.10	283.44	238.83	256.14
$\sigma_{a,20} \ (\mathrm{cm/s^2})$	23.06	21.15	19.76	21.13	16.61
$\sigma_{a,40} \ (\mathrm{cm/s^2})$	43.94	26.01	37.76	22.73	30.26
$\sigma_{a,60} \ (\mathrm{cm/s^2})$	82.57	48.80	71.13	43.04	57.01
$\overline{P_g}$ (kW)	-	111.54	40.51	104.60	81.08
$E_g$ (kWh)	-	6.20	2.25	5.81	4.50
$E_{in}$ (kWh)	8.80	9.16	9.09	7.93	9.23
$E_r$ (%)	-	67.7	24.8	73.3	48.8

Table 2: Result for Tokachioki

susceptible to the higher modes whose peaks the TIMET does not reduce as shown in Figure 3 as stated previously.

The time histories of the relative displacements of the 60th floor and the generated powers obtained from the parameters for  $\mu = 0.1$  are compared in Figures 5, 6, and 7. In these figures, the superiorities of the TIMET over the ET can be found in both mitigating response displacements and improving energy absorbing efficiency to the long period earthquakes. Thus these results show that the validity of the TIMET designed to reduces the peak of the magnitude of the 1st mode intensively as shown in Figure 3 for the high-rise building subject to the long period earthquakes.

#### 6. Conclusions

The primary purpose of this paper is to introduced the outrigger tuned inertial mass electromagnetic transducer (TIMET) for the purpose of the seismic protection of high-rise buildings. The analytical model for the proposed system was developed and the magnitude of the transfer function showed that the peak of the 1st mode of the high-rise building was reduced significantly. Also the effectiveness of the proposed outrigger tuned inertial mass mechanism to long period earthquake excitations for vibration response reduction was observed in the time history response analyses. At the same time, it was demonstrated that the outrigger TIMET improves energy generation efficiency to a large extent with the input energy to the structure kept low.

	Uncontrolled	TIMET (I)	ET(I)	TIMET (II)	ET (II)
$p_{x,20} (cm)$	2.25	1.22	2.06	1.05	1.75
$p_{x,40} ({\rm cm})$	7.56	4.09	6.96	3.51	5.95
$p_{x,60} ({\rm cm})$	13.99	7.51	12.88	6.37	11.02
$\sigma_{x,20} \ (\mathrm{cm})$	0.75	0.44	0.67	0.35	0.55
$\sigma_{x,40} \ (\mathrm{cm})$	2.49	1.44	2.21	1.13	1.84
$\sigma_{x,60} \ ({\rm cm})$	4.56	2.60	4.05	2.03	3.36
$p_{a,20} \; ({\rm cm/s^2})$	9.94	8.89	9.09	8.48	8.00
$p_{a,40} \; ({\rm cm/s^2})$	10.85	7.26	9.86	6.90	8.38
$p_{a,60} \ ({\rm cm/s^2})$	24.28	15.25	21.89	13.28	18.31
$\sigma_{a,20} \ (\mathrm{cm/s^2})$	2.06	1.92	1.77	1.85	1.53
$\sigma_{a,40} \ (\mathrm{cm/s^2})$	3.51	2.34	3.07	1.97	2.53
$\sigma_{a,60} \ (\mathrm{cm/s^2})$	6.82	4.68	6.00	4.02	5.01
$\overline{P_g}$ (kW)	-	1.04	0.29	0.99	0.65
$E_{g}$ (kWh)	-	0.05	0.01	0.04	0.03
$E_{in}$ (kWh)	0.05	0.07	0.05	0.06	0.06
$E_r$ (%)	-	65.9	24.6	71.6	49.0

Table 3: Result for Tohoku

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	Uncontrolled	TIMET (I)	ET(I)	TIMET (II)	ET (II)
$p_{x,20} (cm)$	22.57	12.46	19.63	9.30	15.72
$p_{x,40} ({\rm cm})$	74.69	41.01	65.00	30.42	51.80
$p_{x,60} ({\rm cm})$	136.67	74.72	118.99	55.26	94.54
$\sigma_{x,20} \ (\mathrm{cm})$	5.70	2.83	4.85	2.36	3.83
$\sigma_{x,40} \ (\mathrm{cm})$	18.84	9.28	16.03	7.68	12.64
$\sigma_{x,60} \ (\mathrm{cm})$	34.46	16.96	29.31	13.99	23.10
$p_{a,20} \ ({\rm cm/s^2})$	117.09	112.86	89.21	117.04	68.02
$p_{a,40} \; ({\rm cm/s^2})$	100.30	78.53	88.86	80.74	71.42
$p_{a,60} \; ({\rm cm/s^2})$	190.76	186.57	165.94	184.49	134.09
$\sigma_{a,20} \ ({\rm cm/s^2})$	14.28	13.75	12.16	15.08	9.94
$\sigma_{a,40} \ (\mathrm{cm/s^2})$	26.80	15.69	22.74	14.80	17.96
$\sigma_{a,60} \ (\mathrm{cm/s^2})$	50.35	30.16	42.43	29.61	32.98
$\overline{P_g}$ (kW)	-	32.55	14.09	33.71	26.56
$E_g$ (kWh)	-	5.43	2.35	5.62	4.43
$E_{in}$ (kWh)	9.59	8.32	9.47	7.96	9.08
$E_r$ (%)	-	65.2	24.8	70.6	48.7

Table 4: Result for Nankai Trough

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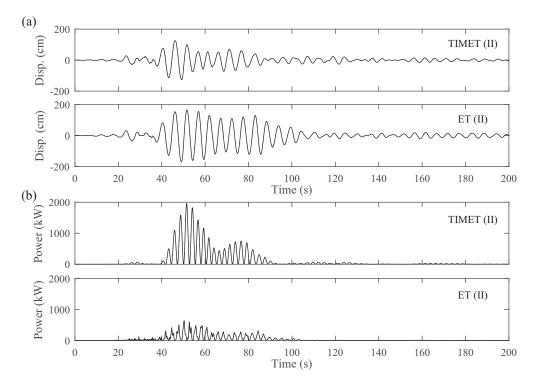


Figure 5: Time histories for Tokachioki: (a) Displacement of the 60th floor, (b) Generated power.

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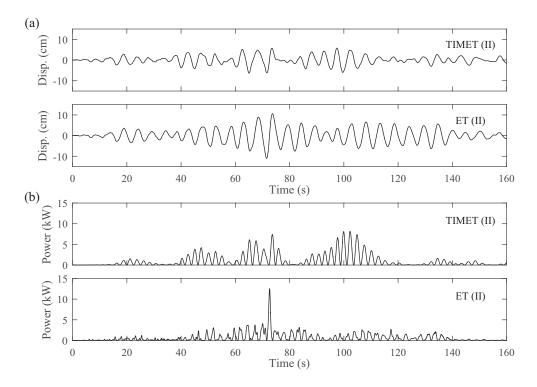


Figure 6: Time histories for Tohoku: (a) Displacement of the 60th floor, (b) Generated power.

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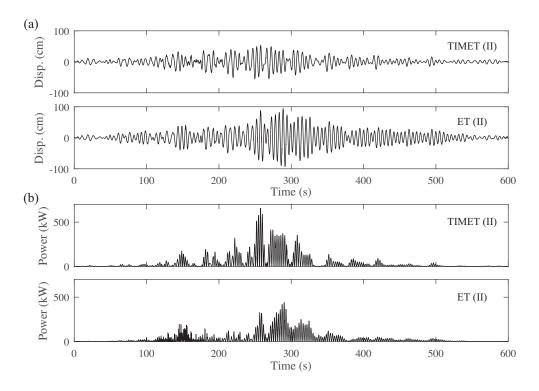


Figure 7: Time histories for Nankai Trough: (a) Displacement of the 60th floor, (b) Generated power.

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