## Observation of $\boldsymbol{B}_{s}^{\mathbf{0}}-\overline{\boldsymbol{B}}_{s}^{\mathbf{0}}$ Oscillations

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We report the observation of $B_{s}^{0}-\bar{B}_{s}^{0}$ oscillations from a time-dependent measurement of the $B_{s}^{0}-\bar{B}_{s}^{0}$ oscillation frequency $\Delta m_{s}$. Using a data sample of $1 \mathrm{fb}^{-1}$ of $p \bar{p}$ collisions at $\sqrt{s}=1.96 \mathrm{TeV}$ collected with the CDF II detector at the Fermilab Tevatron, we find signals of 5600 fully reconstructed hadronic $B_{s}$ decays, 3100 partially reconstructed hadronic $B_{s}$ decays, and 61500 partially reconstructed semileptonic $B_{s}$ decays. We measure the probability as a function of proper decay time that the $B_{s}$ decays with the same, or opposite, flavor as the flavor at production, and we find a signal for $B_{s}^{0}-\bar{B}_{s}^{0}$ oscillations. The probability that random fluctuations could produce a comparable signal is $8 \times 10^{-8}$, which exceeds $5 \sigma$ significance. We measure $\Delta m_{s}=17.77 \pm 0.10($ stat $) \pm 0.07($ syst $) \mathrm{ps}^{-1}$ and extract $\left|V_{\mathrm{td}} / V_{\mathrm{ts}}\right|=0.2060 \pm$ $0.0007\left(\Delta m_{s}\right)_{-0.0060}^{+0.0081}\left(\Delta m_{d}+\right.$ theor $)$.

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Since the first observation of particle-antiparticle transformations in neutral $B$ mesons in 1987 [1], the determination of the $B_{s}^{0}-\bar{B}_{s}^{0}$ oscillation frequency $\Delta m_{s}$ from a timedependent measurement of $B_{s}^{0}-\bar{B}_{s}^{0}$ oscillations has been a major objective of experimental particle physics [2]. This frequency can be used to extract the magnitude of $V_{t s}$, one of the nine elements of the Cabibbo-Kobayashi-Maskawa
(CKM) matrix [3]. Recently, we reported [4] the strongest evidence to date of the direct observation of $B_{s}^{0}-\bar{B}_{s}^{0}$ oscillations. That analysis used $1 \mathrm{fb}^{-1}$ of data collected with the CDF II detector [5] at the Fermilab Tevatron, and the probability that random fluctuations would produce a comparable signal was $0.2 \%$, corresponding to $3 \sigma$ signal significance. This level of significance is insufficient to claim

TABLE I. Signal yields $(S)$ and signal to background ratio $(S / B)$ in the various hadronic decay sequences. The gain refers to the percentage increase in $S / \sqrt{S+B}$ relative to [4].

| Decay Sequence | Signal | $S / B$ | Gain, with respect to [4] |
| :--- | :---: | :---: | :---: |
| $\bar{B}_{s}^{0} \rightarrow D_{s}^{+}\left(\phi \pi^{+}\right) \pi^{-}$ | 2000 | 11.3 | $13 \%$ |
| Partially reconstructed | 3100 | 3.4 | $\ldots$ |
| $\bar{B}_{s}^{0} \rightarrow D_{s}^{+}\left(\bar{K}^{*}(892)^{0} K^{+}\right) \pi^{-}$ | 1400 | 2.0 | $35 \%$ |
| $\bar{B}_{s}^{0} \rightarrow D_{s}^{+}\left(\pi^{+} \pi^{-} \pi^{+}\right) \pi^{-}$ | 700 | 2.1 | $22 \%$ |
| $\bar{B}_{s}^{0} \rightarrow D_{s}^{+}\left(\phi \pi^{+}\right) \pi^{-} \pi^{+} \pi^{-}$ | 700 | 2.7 | $92 \%$ |
| $\bar{B}_{s}^{0} \rightarrow D_{s}^{+}\left(\bar{K}^{*}(892)^{0} K^{+}\right) \pi^{-} \pi^{+} \pi^{-}$ | 600 | 1.1 | $110 \%$ |
| $\bar{B}_{s}^{0} \rightarrow D_{s}^{+}\left(\pi^{+} \pi^{-} \pi^{+}\right) \pi^{-} \pi^{+} \pi^{-}$ | 200 | 2.6 | $\ldots$ |

a firm observation; however, under the oscillation hypothesis we determined $\Delta m_{s}=17.31_{-0.18}^{+0.33}($ stat $) \pm$ 0.07 (syst) $\mathrm{ps}^{-1}$. In this Letter we report an update of this measurement that uses the same data set with an improved analysis and reduces this probability to $8 \times 10^{-8}(>5 \sigma)$, yielding the first definitive observation of time-dependent $B_{s}^{0}-\bar{B}_{s}^{0}$ oscillations.

We improve the analysis in Ref. [4] by increasing the $B_{s}$ signal yield and improving the performance of the methods used to identify the flavor ( $b$ or $\bar{b}$ ) of the $B_{s}$ at production. The previous analysis used $B_{s}$ decays in hadronic ( $\bar{B}_{s}^{0} \rightarrow$ $\left.D_{s}^{+} \pi^{-}, \quad D_{s}^{+} \pi^{-} \pi^{+} \pi^{-}\right) \quad$ and $\quad$ semileptonic $\quad\left(\bar{B}_{s}^{0} \rightarrow\right.$ $D_{s}^{+(*)} \ell^{-} \bar{\nu}_{\ell}, \ell=e$ or $\mu$ ) decay modes [6]. We used $D_{s}^{+} \rightarrow$ $\phi \pi^{+}, \bar{K}^{*}(892)^{0} K^{+}$, and $\pi^{+} \pi^{-} \pi^{+}$, with $\phi \rightarrow K^{+} K^{-}$and $\bar{K}^{* 0} \rightarrow K^{-} \pi^{+}$. Several improvements lead to increased signal yields. We use particle-identification techniques to find kaons from $D_{s}$ meson decays, allowing us to relax kinematic selection requirements on the $D_{s}$ decay products. This results in increased efficiency for reconstructing the $D_{s}$ while maintaining excellent signal to background. In the hadronic channels, we employ an artificial neural
network (ANN) to improve candidate selection resulting in larger signal yields at similar or smaller background levels. The ANN selection makes it possible to use the additional decay sequence $\bar{B}_{s}^{0} \rightarrow D_{s}^{+} \pi^{-} \pi^{+} \pi^{-}$, with $D_{s}^{+} \rightarrow$ $\pi^{+} \pi^{-} \pi^{+}$, as well. We add significant statistics using partially reconstructed hadronic decays in which a photon or $\pi^{0}$ is missing: $\bar{B}_{s}^{0} \rightarrow D_{s}^{*+} \pi^{-}, D_{s}^{*+} \rightarrow D_{s}^{+} \gamma / \pi^{0}$ and $\bar{B}_{s}^{0} \rightarrow D_{s}^{+} \rho^{-}, \rho^{-} \rightarrow \pi^{-} \pi^{0}$, with $D_{s}^{+} \rightarrow \phi \pi^{+}$. Finally ANNs are used to enhance the performance of the methods used to identify the flavor of the $B_{s}$ at production.

To reconstruct $\bar{B}_{s}^{0}$ candidates, we first select $D_{s}^{+}$candidates. These $D_{s}^{+}$candidates are combined with one or three additional charged particles to form $D_{s}^{+} \ell^{-}, D_{s}^{+} \pi^{-}$, or $D_{s}^{+} \pi^{-} \pi^{+} \pi^{-}$candidates. In the previous analysis, we reduced combinatorial backgrounds by applying requirements on selection quantities such as the minimum $p_{T}$ [7] of the $\bar{B}_{s}^{0}$ and its decay products, and the quality of the reconstructed $\bar{B}_{s}^{0}$ and $D_{s}^{+}$decay points and their displacement from the $p \bar{p}$ collision position. In this analysis, we add a kaon identification likelihood formed from time-offlight and $d E / d x$ information. For decay modes with kaons


FIG. 1. Left panel: the invariant mass distributions for the $D_{s}^{+}\left(\phi \pi^{+}\right)$candidates [inset] and the $\ell^{-} D_{s}^{+}\left(\phi \pi^{+}\right)$pairs. The contribution labeled "false lepton \& physics" (dashed line) refers to backgrounds from hadrons mimicking the lepton signature combined with real $D_{s}$ mesons and physics backgrounds such as $B^{0} \rightarrow D_{s}^{+} D^{-}, D_{s_{-}}^{+} \rightarrow \phi \pi^{+}, D^{-} \rightarrow \ell^{-} X$. Right panel: the invariant mass distribution for $\bar{B}_{s}^{0} \rightarrow D_{s}^{+}\left(\phi \pi^{+}\right) \pi^{-}$decays including the contributions from $\bar{B}_{s}^{0} \rightarrow D_{s}^{*+} \pi^{-}$and $\bar{B}_{s}^{0} \rightarrow D_{s}^{+} \rho^{-}$. In this panel, signal contributions are drawn added on top of the combinatorial background.


FIG. 2. The invariant mass distributions for $\bar{B}_{s}^{0} \rightarrow D_{s}^{+} \pi^{-}$(top panels) and $D_{s}^{+} \pi^{-} \pi^{+} \pi^{-}$(bottom panels). Signal contributions are added on top of the combinatorial background. Contributions from partially reconstructed $B_{s}$ decays are taken into account in the fit and are not shown.
in the final state, we use this likelihood to reduce combinatorial background from random pions or physics backgrounds such as $D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$. In [4], we vetoed $D_{s}^{+}$ candidates consistent with the $D^{+}$mass hypothesis, which resulted in a substantial loss of signal efficiency. Kaon identification makes it possible to relax kinematic requirements (charged particle $p_{T}$ and the $D^{+}$veto) leading to a substantial increase in signal efficiency.

In the semileptonic channel, the main gain is in the $D_{s}^{+} \ell^{-}, D_{s}^{+} \rightarrow \bar{K}^{*}(892)^{0} K^{+}$sequence, where the signal is increased by a factor of 2.2. An additional gain in signal by a factor of 1.3 with respect to our previous analysis comes from adding data selected with different trigger requirements. In total the signal of 37000 semileptonic $B_{s}$ decays in [4] is increased to 61500 , and the signal to background improves by a factor of 2 in the sequences with kaons in the final state. The distributions of the invariant masses of the $D_{s}^{+}\left(\phi \pi^{+}\right) \ell^{-}$pairs $m_{D_{s} \ell}$ and the $D_{s}^{+}\left(\phi \pi^{+}\right)$candidates are shown in Fig. 1. We use $m_{D_{s} \ell}$ to help distinguish signal, which occurs at higher $m_{D_{s} \ell}$, from combinatorial and physics (e.g., double-charm decays of $B$ mesons) backgrounds.

In the hadronic decay modes, we use an ANN to enhance the signal selection of the previous analysis. The ANN uses quantities such as the selection criteria listed above as well as the kaon identification likelihood. The network is trained using simulated signals generated with Monte Carlo methods. For combinatorial background, we use sideband regions in the mass distribution of the $B_{s}$ candidates from data. In this analysis, we add the partially reconstructed signal between 5.0 and $5.3 \mathrm{GeV} / c^{2}$ from $\bar{B}_{s}^{0} \rightarrow D_{s}^{*+} \pi^{-}, D_{s}^{*+} \rightarrow D_{s}^{+} \gamma / \pi^{0}$ in which a photon or $\pi^{0}$ from the $D_{s}^{*+}$ is missing and $\bar{B}_{s}^{0} \rightarrow D_{s}^{+} \rho^{-}, \rho^{-} \rightarrow \pi^{-} \pi^{0}$ in which a $\pi^{0}$ is missing. The mass distributions for $\bar{B}_{s}^{0} \rightarrow$ $D_{s}^{+} \pi^{-}, D_{s}^{+} \rightarrow \phi \pi^{+}$and the partially reconstructed signals are shown in Fig. 1. The mass distributions for the other five hadronic decay sequences are shown in Fig. 2. In these modes, we require the masses of the candidates to be greater than $5.3 \mathrm{GeV} / c^{2}$. Candidates with masses greater than $5.5 \mathrm{GeV} / c^{2}$ are used to construct probability density functions (PDFs) for combinatorial background. Table I summarizes the signal yields.

The reconstructed decay time in the $B_{s}$ rest frame is $t=$ $m_{B_{s}} L_{T} / p_{T}^{\text {recon }}$, where $L_{T}$ is the displacement of the $B_{s}$


FIG. 3. Left panel: the distribution of the correction factor $\kappa$ in semileptonic and partially reconstructed hadronic decays from Monte Carlo simulation. Right panel: the average proper decay-time resolution for $B_{s}$ decays as a function of proper decay time.
decay point with respect to the primary vertex projected onto the $B_{s}$ transverse momentum vector, and $p_{T}^{\text {recon }}$ is the transverse momentum of the reconstructed decay products. In the semileptonic and partially reconstructed hadronic decays, we correct $t$ by a factor $\kappa=p_{T}^{\mathrm{recon}} / p_{T}\left(B_{s}\right)$ determined with Monte Carlo simulation (Fig. 3).

The decay-time resolution $\sigma_{t}$ has contributions from the momentum of missing decay products (due to the spread of the distribution of $\kappa$ ) and from the uncertainty on $L_{T}$. The uncertainty due to the missing momentum increases with proper decay time and is an important contribution to $\sigma_{t}$ in the semileptonic decays. To reduce this contribution and make optimal use of the semileptonic decays, we determine the $\kappa$ distribution as a function of $m_{D_{s} \ell}$ (Fig. 3). We estimate the contribution from the uncertainty on $L_{T}$ to $\sigma_{t}$ for each candidate using the measured track parameters and their estimated uncertainties.

The distribution of $\sigma_{t}$ for fully reconstructed decays has an average value of 87 fs , which corresponds to one fourth of an oscillation period at $\Delta m_{s}=17.8 \mathrm{ps}^{-1}$. The distribution is nearly Gaussian with an rms width of 31 fs . For the partially reconstructed hadronic decays, the average $\sigma_{t}$ is 97 fs , and the addition to $\sigma_{t}$ due to the missing photon or $\pi^{0}$ is very small (Fig. 3). For semileptonic decays, $\sigma_{t}$ is worse due to decay topology and the much larger missing momentum of decay products that were not reconstructed. The increase of $\sigma_{t}$ with $t$ is illustrated in Fig. 3 for different ranges of $m_{D_{s}} \ell$.

The flavor of the $B_{s}$ at production is determined using both opposite-side and same-side flavor tagging techniques. The effectiveness $Q \equiv \epsilon \mathcal{D}^{2}$ of these techniques is quantified with an efficiency $\epsilon$, the fraction of signal candidates with a flavor tag, and a dilution $\mathcal{D} \equiv 1-2 w$, where $w$ is the probability that the tag is incorrect.

At the Tevatron, the dominant $b$-quark production mechanisms produce $b \bar{b}$ pairs. Opposite-side tags infer the production flavor of the $B_{s}$ from the decay products of the $b$ hadron produced from the other $b$ quark in the event. In the previous analysis, we used lepton ( $e$ and $\mu$ ) charge and jet charge as tags, and if both types of tag were present, we used the lepton tag. In this improved analysis, we add an opposite-side flavor tag based on the charge of identified kaons [8], and we combine the information from the kaon, lepton, and jet-charge tags using an ANN. The dilution is measured in data [9] using large samples of $B^{-}$ and $\bar{B}^{0}$ mesons. The combined opposite-side tag effectiveness improves by $20 \%$ to $Q=1.8 \pm 0.1 \%$. Most of the improvement is for candidates with both a lepton and jetcharge tag.

Same-side flavor tags are based on the charges of associated particles produced in the fragmentation of the $b$ quark that produces the reconstructed $B_{s}$. In the previous analysis, we used a same-side tag based on our kaon particle-identification likelihood; here we use an ANN to combine our kaon particle-identification likelihood with
kinematic quantities of the kaon candidate into a single tagging variable $T$. Tracks close in phase space to the $B_{s}$ candidate are considered as same-side kaon tag candidates, and the track with the largest value of $T$ is selected as the tagging track. We predict the dilution of the same-side tag using simulated data samples generated with the PYTHIA Monte Carlo [10] program. The predicted fractional gain in $Q$ from using the ANN is $10 \%$. Control samples of $B^{-}$and $\bar{B}^{0}$ are used to validate the predictions of the simulation. The effectiveness of this flavor tag increases with the $p_{T}$ of the $\bar{B}_{s}^{0}$; we find $Q=3.7 \%$ ( $4.8 \%$ ) in the hadronic (semileptonic) decay sample. The fractional uncertainty on $Q$ is approximately $25 \%$ [4]. If both a same-side tag and an opposite-side tag are present, we combine the information from both tags assuming they are independent.

We use an unbinned maximum likelihood fit to search for $B_{s}$ oscillations. The likelihood combines mass, decay time, decay-time resolution, and flavor tagging information for each candidate, and includes terms for signal and each type of background. Details of the fit are described in [4,11].

Following the method described in [12], we fit for the oscillation amplitude $\mathcal{A}$ while fixing $\Delta m_{s}$ to a probe value. The oscillation amplitude is expected to be consistent with $\mathcal{A}=1$ when the probe value is the true oscillation frequency, and consistent with $\mathcal{A}=0$ when the probe value is far from the true oscillation frequency. Figure 4 shows the fitted value of the amplitude as a function of the oscillation frequency for the semileptonic candidates alone, the hadronic candidates alone, and the combination. The sensitivity [4,12] is $19.3 \mathrm{ps}^{-1}$ for the semileptonic decays alone, $30.7 \mathrm{ps}^{-1}$ for the hadronic decays alone, and $31.3 \mathrm{ps}^{-1}$ for all decays combined. At $\Delta m_{s}=$ $17.77 \mathrm{ps}^{-1}$, the observed amplitude $\mathcal{A}=1.21 \pm$ 0.20 (stat) is consistent with unity, indicating that the data are compatible with $B_{s}^{0}-\bar{B}_{s}^{0}$ oscillations with that frequency, while the amplitude is inconsistent with zero: $\mathcal{A} / \sigma_{\mathcal{A}}=$ 6.05, where $\sigma_{\mathcal{A}}$ is the statistical uncertainty on $\mathcal{A}$ (the ratio has negligible systematic uncertainties).

We evaluate the significance of the signal using $\Lambda \equiv$ $\log \left[\mathcal{L}^{\mathcal{A}=0} / \mathcal{L}^{\mathcal{A}=1}\left(\Delta m_{s}\right)\right]$, which is the logarithm of the ratio of likelihoods for the hypothesis of oscillations ( $\mathcal{A}=$ 1) at the probe value and the hypothesis that $\mathcal{A}=0$, which is equivalent to random production flavor tags. Figure 4 shows $\Lambda$ as a function of $\Delta m_{s}$. Separate curves are shown for the semileptonic data alone (dashed), the hadronic data alone (light solid), and the combined data (dark solid). At the minimum $\Delta m_{s}=17.77 \mathrm{ps}^{-1}, \Lambda=-17.26$. The significance of the signal is the probability that randomly tagged data would produce a value of $\Lambda$ lower than -17.26 at any value of $\Delta m_{s}$. We repeat the likelihood scan $350 \times 10^{6}$ times with random tagging decisions; 28 of these scans have $\Lambda<-17.26$, corresponding to a probability of $8 \times 10^{-8}(5.4 \sigma)$, well below $5.7 \times 10^{-7}$ ( $5 \sigma$ ).



FIG. 4. The measured amplitude values and uncertainties versus the $B_{s}^{0}-\bar{B}_{s}^{0}$ oscillation frequency $\Delta m_{s}$. Upper left: semileptonic decays only. (Lower Left) hadronic decays only. Upper right: all decay modes combined. Lower right: the logarithm of the ratio of likelihoods for amplitude equal to one and amplitude equal to zero, $\Lambda=\log \left[\mathcal{L}^{\mathcal{A}=0} / \mathcal{L}^{\mathcal{A}=1}\left(\Delta m_{s}\right)\right]$, versus the oscillation frequency. The horizontal line indicates the value $\Lambda=-15$ that corresponds to a probability of $5.7 \times 10^{-7}(5 \sigma)$ in the case of randomly tagged data.

To measure $\Delta m_{s}$, we fix $\mathcal{A}=1$ and fit for the oscillation frequency. We find $\Delta m_{s}=17.77 \pm 0.10$ (stat) $\pm$ 0.07 (syst) $\mathrm{ps}^{-1}$. The only non-negligible systematic uncertainty on $\Delta m_{s}$ is from the uncertainty on the absolute scale of the decay-time measurement. Contributions to this uncertainty include biases in the primary-vertex reconstruction due to the presence of the opposite-side $b$ hadron, uncertainties in the silicon-detector alignment, and biases in track fitting. The uncertainty on the correction $\kappa$ for the hadronic candidates with a missing photon or $\pi^{0}$ is included and has a negligible effect.

The $B_{s}^{0}-\bar{B}_{s}^{0}$ oscillations are depicted in Fig. 5. Candidates in the hadronic sample are collected in five bins of proper decay-time modulo the measured oscillation period $2 \pi / \Delta m_{s}$. In each bin, we fit for an amplitude (the points in Fig. 5) using the likelihood function [4], which takes into account the effects of background, flavor tag dilution and decay-time resolution for each candidate. The curve shown in Fig. 5 is a cosine with an amplitude of 1.28 , which is the observed value in the amplitude scan for the hadronic sample at $\Delta m_{s}=17.77 \mathrm{ps}^{-1}$. As expected, the data are well represented by the curve.

The measured $B_{s}^{0}-\bar{B}_{s}^{0}$ oscillation frequency is used to derive the ratio $\left|V_{\mathrm{td}} / V_{\mathrm{ts}}\right|=\xi \sqrt{\frac{\Delta m_{d}}{\Delta m_{s}} \frac{m_{B_{s}^{0}}}{m_{B^{0}}}}$ [13]. As inputs we use $m_{B^{0}} / m_{B_{s}^{0}}=0.98390$ [14] with negligible uncertainty, $\Delta m_{d}=0.507 \pm 0.005 \mathrm{ps}^{-1}$ [13] and $\xi=1.21_{-0.035}^{+0.047}$ [15]. We find $\left|V_{\mathrm{td}} / V_{\mathrm{ts}}\right|=0.2060 \pm 0.0007\left(\Delta m_{s}\right)_{-0.0060}^{+0.0081}\left(\Delta m_{d}+\right.$ theor).

In conclusion, we report the first observation of $B_{s}^{0}-\bar{B}_{s}^{0}$ oscillations from a decay-time-dependent measurement of $\Delta m_{s}$. Our signal exceeds $5 \sigma$ significance and yields a precise value of $\Delta m_{s}$, which is consistent with standard model expectations. This result supersedes our previous measurement [4].


FIG. 5. The $B_{s}^{0}-\bar{B}_{s}^{0}$ oscillation signal measured in five bins of proper decay-time modulo the measured oscillation period $2 \pi / \Delta m_{s}$. The figure is described in the text.

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