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Physical Review Letters

Volume 108

Number 22

Page Range 227401

Year 2012

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URL http://hdl.handle.net/2241/117352
doi: 10.1103/PhysRevLett.108.227401
Multiple Exciton Generation by a Single Photon in Single-Walled Carbon Nanotubes

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(Received 21 July 2011; published 29 May 2012)

Multiple-exciton generation in single-walled carbon nanotubes is investigated theoretically. We show that multiple excitons can be directly generated by a single photon through resonant coupling with multie exciton states. Further, the theoretically predicted threshold energy for this process is consistent with recent experimental results. Our calculations clarify the elementary processes of multiple-exciton generation in single-walled carbon nanotubes.

DOI: 10.1103/PhysRevLett.108.227401
PACS numbers: 78.67.Ch, 71.35.Cc

To realize an environmentally sustainable society, it is important to develop novel devices that have low energy consumptions to reduce the depletion of natural energy sources. It is also important to investigate and develop clean, renewable natural energy sources. Solar power is one of the most promising inexhaustible natural energy sources. In recent decades, much effort has been devoted to developing solar cells and to increasing their energy conversion efficiencies. Although recent technical progress has made it possible to utilize solar cells to power industrial applications, Shockley and Queisser [1] revealed that has made it possible to utilize solar cells to power industrial applications. Shockley and Queisser [1] revealed that the fundamental limit on the energy conversion efficiency, which is determined by the detailed balance of various processes.

Of the various processes that contribute to energy dissipation, photoelectric conversion mainly determines the energy conversion efficiency of cells. In conventional bulk semiconductors, a single electron-hole pair or an exciton is generated on the absorption of a single photon whose energy exceeds that of the energy gap between the conduction and valence bands. In this process, the surplus photon energy is dissipated through phonon emission as heat. However, two or more electron-hole pairs or excitons can be generated through energy transfer mediated by the Coulomb interaction if such a process can be much more efficient than the dissipative process associated with phonons. It is known as multiple-exciton generation (MEG). Since it generates two or more electron-hole pairs, MEG may substantially enhance the energy conversion efficiency. It is thus important to clarify the underlying process of MEG, not only to develop next-generation photovoltaic devices that exceed the Shockley-Queisser limit, but also to understand the fundamental physics of strongly interacting many-body excited states.

It was predicted that MEG is efficient in semiconducting nanocrystals due to inefficient phonon emission, known as the phonon bottleneck [2]. The discretized energy levels of semiconducting nanocrystals hinder resonance with the phonon energy due to the energy differences that exist between these levels. Furthermore, while energy is conserved, momentum is not necessarily conserved due to the absence of translational symmetry in the nanocrystals. Therefore, in semiconducting nanocrystals, MEG overcomes the relaxation of photoexcited states caused by phonon emission. Indeed, MEG has been experimentally observed in several semiconductor nanocrystals [3–6]. However, contrary to the above reports, recent experiments indicate that MEG in confined materials does not exceed the efficiency in the corresponding bulk systems [7–12]. While various theories have been proposed regarding the efficiency and the threshold energy, the mechanism of MEG in semiconducting nanocrystals is still controversial [13–20].

In addition to semiconducting nanocrystals, single-walled carbon nanotubes (SWNTs) are another possible system for investigating MEG since their quasi-one-dimensional structure gives rise to a substantial Coulomb interaction [21–23]. SWNTs can be used to systematically analyze the fundamental mechanism of MEG since their sizes and structures have been well characterized. One of the most important difference between nanocrystals and SWNTs is the conservation restriction applying for the MEG process. The MEG of nanocrystals obeys only energy conservation, while the MEG of SWNTs obeys the energy conservation, momentum conservation, and the angular momentum conservation. The difference of dimensionality, accordingly, can allow us to determine the microscopic processes of MEG in SWNTs. MEG has recently been observed in SWNTs by transient absorption spectroscopy [24,25] and photocurrent spectroscopy [26]. However, as is the case with semiconductor nanocrystals, the underlying physics of MEG in SWNTs has not yet been determined.

In this study, we, thus, theoretically determine the fundamental process of MEG in SWNTs. We show that MEG occurs in SWNTs by the direct photogeneration of multiple excitons. In addition, we also demonstrate that the high efficiency of MEG is due to the strong Coulomb interaction between excitons and to a singularity in the density of states of multiple-exciton states. This study provides a
We consider direct photo-induced generation of multiple excitons. Of the various possible multiple-exciton states, we consider only two-exciton final states. A single photon can generate two excitons due to resonant coupling between the single-exciton state and the multiple-exciton state induced by the Coulomb interaction. The perturbation theory has successfully explained, for instance, the Auger recombination rate of excitons in SWNTs [27], which justified the perturbation treatment of the Coulomb interaction between interacting excitons. After utilizing the first order perturbation regarding the Coulomb interaction $V$, the ground state $|g\rangle$ becomes

$$
|g\rangle = |g\rangle + \sum_\mu |\mu\rangle \frac{\langle \mu | V | g\rangle}{E_0 - E_\mu} + \sum_\mu, \nu |\mu ; \nu\rangle \frac{\langle \mu; \nu | V | g\rangle}{E_0 - E_{\mu, \nu}},
$$

and the two-exciton state, $|\mu ; \nu\rangle$, becomes

$$
|\mu ; \nu\rangle = |\mu; \nu\rangle + \sum_\mu |\mu\rangle \frac{\langle \mu | V | \mu ; \nu\rangle}{E_\mu - E_{\mu, \nu}} \times \sum_\mu', \nu' \not\equiv \mu, \nu |\mu'; \nu'\rangle \frac{\langle \mu'; \nu' | V | \mu; \nu\rangle}{E_{\mu', \nu'} - E_{\mu, \nu}}.
$$

In the above equations, $|\mu\rangle \equiv |n, q\rangle$ and $|\mu; \nu\rangle \equiv |n, q; n', q'\rangle \equiv |n, q \otimes n', q'\rangle$, where $|n, q\rangle = \sum_k Z_k^n e_k c_{k, n} c_{k, q}$ is the nth exciton state with momentum $q$ whose energy is denoted by $E_\mu = E_q$. The energy of two-exciton state is defined by $E_{\mu, \nu} = E_q + E_{q'}$. Here, $c_{(n)}$ is the annihilation operators for an electron in the conduction (valence) band. The amplitude of excitons, $Z_k^n$, and its energy $E_q^n$ are determined below by solving the Bethe-Salpeter equation.

As a result of the Coulomb interaction, the multiple-exciton state can directly couple to the ground state by absorbing a single photon, i.e., $|g\rangle \mathcal{H}_{op} |\mu; \nu\rangle \neq 0$. The direct generation of two excitons by a single photon is necessarily conserved between the intermediate and final states. Direct generation of the two-exciton state $|1, q; 1, -q\rangle$ via the exciton-photon interaction $\mathcal{H}_{op}$ is forbidden.

$$
\epsilon_{k+q} - \epsilon_k + \sum_{k'} K_{k,k'} Z_{k,q} \epsilon_{k'} = E_q^0 Z_{k,q}.
$$

where $K_{k,k'}$ is the Coulomb interaction kernel that consists of bare-exchange and screened-direct terms. The quasiparticle energies $\epsilon_k^0$ and $\epsilon_k^{\pi}$ are calculated by applying the random-phase approximation [21, 22, 28, 29]. For the Coulomb potential between $\pi$ orbitals, we employed the Ohno potential $V(r) = U/\kappa \sqrt{\frac{4\pi e^2}{c} U |r|^2 + 1}$ with $U = 11.3$ eV, which has been known to realistically describe optical responses in single-walled carbon nanotubes [22, 28–30]. The dielectric function $\kappa = 3.3$ was used to incorporate screening effects by $\sigma$ electrons and the surrounding environment. The calculations were performed under the tight-binding approximation by accounting for nearest-neighbor hopping of 3.0 eV. We consider a chirality of (17, 0) as a representative of SWNTs.

We start with the conversion rates for one and two-exciton generation. The one-exciton generation rate is given by
\[ \Gamma_s(\omega) = \frac{2\pi}{\hbar} \sum_n |\langle n, 0|H_{op}|g\rangle|^2 \delta(\hbar \omega - E_n^0). \]  

This is related to linear absorption spectra. Figure 2 shows the conversion rates calculated from Eqs. (3) and (5). The spectral profile for one-exciton generation has the usual structure of the linear absorption spectrum with peaks for the lowest exciton state \( E_{11} \) and higher states and a continuum for excitons above the band gap. In contrast, two-exciton generation increases abruptly at the threshold energy, which corresponds to twice the lowest exciton energy (i.e., \( 2E_{11} \)). As mentioned above, the threshold energy is solely determined by energy conservation expressed by the Dirac delta function in Eq. (3). Further increasing the excitation energy rapidly reduces the rate. The nature of the spectrum for two-exciton generation can be explained by considering the density of states of the two-exciton state. Because of the quasi-one-dimensional structure of SWNTs, the density of states for excitons possesses van Hove singularities. Thus, the spike at the threshold originates from the van Hove singularity in the density of states for excitons [31]. Furthermore, the rapid reduction in the rates with increasing excitation energy is attributed to a reduction in the density of states. In addition, two-exciton generation strongly depends on the dephasing factor. Figure 2 shows spectra calculated for three representative dephasing factors of \( \gamma = 2.0, 8.0, \) and \( 20.0 \) meV. The MEG rate decreases rapidly with increasing dephasing rate.

The threshold energy for two-exciton generation has only a single peak since we consider only two-exciton generation. If final states with three or more exciton states are considered, other sharp peaks corresponding to multi-exciton generation will appear.

We estimate the conversion efficiency of MEG to investigate whether the process can be used to improve photovoltaic devices. The efficiency is evaluated using the following formula:

\[ \eta(\omega) = 1 + \frac{\Gamma_{\text{MEG}}(\omega)}{\Gamma_s(\omega) + \Gamma_{\text{MEG}}(\omega)}, \]

where \( \Gamma_{\text{MEG}}(\omega) \) and \( \Gamma_s(\omega) \) are defined by Eqs. (3) and (5), respectively. Figure 3 shows the calculated conversion efficiencies for dephasing factors of \( \gamma = 2.0, 8.0, \) and \( 20.0 \) meV. The efficiency reaches 175\% for \( \gamma = 2.0 \) meV, which is close to the maximum efficiency (200\%) for two-exciton generation. This remarkably high efficiency is ascribed to both the van Hove singularity in the density of states of the final states and the strong resonance between the intermediate and final states mediated by the Coulomb interaction, which exceeds the dephasing process represented by \( \gamma \). The MEG efficiency is largest at the threshold energy corresponding to the van Hove singularity, as is the MEG rate (see Fig. 2). Without any dephasing processes, this resonance makes an infinite contribution to the MEG rates. However, as shown in Fig. 3, the MEG efficiency depends strongly on the dephasing factor \( \gamma \) via the numerator of Eq. (3). We note that the linewidth of two-exciton generation peak and the one of single-exciton generation is in generally different with each other. The dephasing rate, \( \gamma \), of MEG expression Eq. (3) determines the linewidth of single-exciton states. Therefore, the linewidth of two-exciton generation peak around \( 2E_{11} \) in Fig. 2 do not change associated with the dephasing rate \( \gamma \).

Figure 4 shows the maximum conversion efficiency of MEG as a function of the dephasing rate. It is important to determine how dephasing affects the conversion efficiency. The efficiency decreases monotonically with increasing dephasing rate.

FIG. 2 (color online). Generation rates for one and two excitons by a single photon. The two-exciton generation rates are calculated for dephasing rates of \( \gamma = 2.0, 8.0, \) and \( 20.0 \) meV. The delta functions in Eqs. (3) and (5) were broadened with a width of \( 20.0 \) meV.

FIG. 3 (color online). Conversion efficiency for direct photogeneration of two excitons plotted for dephasing rates of \( \gamma = 2.0, 8.0, \) and \( 20.0 \) meV.
Multiple carrier generation results from the interaction between excitons competing with phonon dephasing and the van Hove singularity in the density of states of the two-exciton states. Moreover, we have shown that the threshold energy for MEG is exactly $2E_{11}$, which is consistent with recent experimental results. The present study clarifies the microscopic process of MEG in SWNTs. Furthermore, it also clarifies the underlying physics of MEG in other materials. MEG raises the possibility of designing high-efficiency photovoltaic devices with low energy consumptions by using SWNTs as constituent units.

This work was supported by CREST of the Japan Science and Technology Agency and a Grant-in-Aid for Scientific Research from the Ministry of Education, Culture, Sports, Science and Technology (MEXT) of Japan.