Coherence of single spins coupled to a nuclear spin bath of varying density

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Coherence of single spins coupled to a nuclear spin bath of varying density

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The dynamics of single electron and nuclear spins in a diamond lattice with different $^{13}$C nuclear spin concentration is investigated. It is shown that coherent control of up to three individual nuclei in a dense nuclear spin cluster is feasible. The free-induction decays of nuclear spin Bell states and single nuclear coherences among $^{13}$C nuclear spins are compared and analyzed. Reduction in a free-induction-decay time $T_2^*$ and a coherence time $T_2$ upon increase in nuclear spin concentration has been found. For pure diamond, $T_2^*$ as long as 30 $\mu$s and $T_2$ of up to 0.65 ms for the electron spin has been observed. The $^{13}$C concentration dependence of $T_2^*$ is explained by Fermi contact and dipolar interactions with nuclei in the lattice. It has been found that $T_2$ decreases approximately as $1/n$, where $n$ is $^{13}$C concentration, which corresponds to the reported theoretical line of $T_2$ for an electron spin interacting with a nuclear spin bath.

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Defect centers in diamond have attracted considerable interest recently owing to their application for quantum information processing, communication, and metrology, especially the nitrogen-vacancy (NV) center, with its strong and spin-dependent optical transitions that allows for single spin readout and exquisite coherent control, which is crucial for quantum information applications. Owing to the high Debye temperature of diamond and weak coupling to acoustic phonons NV electron spins show long coherence time. It was, e.g., proposed to build small quantum registers by exploiting the interaction between the electron spin and a small number of nuclear spins in the immediate vicinity. Five-qubit would be sufficient to perform all functions necessary for a node in a defect center based quantum repeater node. Up to now coherent control, swapping of coherence, and even entanglement between up to two nuclei and the electron spin were demonstrated. To increase the size of the quantum register, more nuclei need to be coupled to the electron spin. The approach taken here is to increase the concentration of paramagnetic $^{13}$C nuclei in the lattice. We systematically demonstrate coherent control of up to three nuclear spins being coupled to an NV center electron spin in $^{13}$C isotopically enriched crystals, notwithstanding the fact that the electron decoherence time $T_2$ linearly scales with the $^{13}$C concentration. Furthermore, our experiments provide experimental insight into long studied problem of single central spin coupled to a paramagnetic environment. Owing to possibility of addressing individual electron spins in matrix with adjustable nuclear spin content we show the transition from diluted to dense spin bath (the situation relevant for spins in GaAs quantum dots).

The quantum system used in the present work is the negatively charged NV center in diamond, which comprises a substitutional nitrogen atom with an adjacent vacancy. The electron ground state of it is a spin triplet. Upon optical excitation the NV center shows strong fluorescence allowing it to be observed on an individual basis by confocal microscopy. The fluorescence intensity of the defect is spin dependent owing to spin selective relaxation via singlet state, which allows optical read out of the single ESR (Ref. 11) and an efficient electron and nuclear initialization at room temperature. Microwaves (MWs) and radio frequency (RF) fields are used for coherent manipulation of single electron and nuclear spins using conventional ESR/NMR techniques.

FIG. 1. (Color online) Electron-spin resonance (ESR) spectra of single NVs with (a) zero, (b) one, (c) two, and (d) three $^{13}$C in the first shell. Lower solid lines (blue) in (b-d) are simulation spectra. ESR spectra with (e) one and (f) two $^{13}$C in the third shell, and (g) one $^{13}$C in the first shell and one $^{13}$C in the third shell. Blue dashed lines are fitting lines with Gaussian. (h) Atomic structure of NV center. The numbers 1, 2, and 3 mark C in the first shell.
Measurement is carried out at $\sim 20$ °C. Diamond enables for
the unique opportunity to control the concentration of para-
magnetic nuclear spins. The most abundant $^{12}$C has zero
nuclear spin. The concentration of $^{13}$C nuclear spins ($I = 1/2$) can be adjusted to the suitable value by controlling the
isotopic content of $^{13}$C in the growth medium. Two types of
synthetic diamonds were used in this study. Crystals with
0.35%, 1.1%, 8.4%, and 20.7% $^{13}$C concentrations were syn-
thesized by a MW plasma-assisted homoepitaxial chemical
vapor deposition (CVD) (Ref. 12 and 13) technique with
$^{13}$CH$_4$ or $^{12}$CH$_4$ gases. The 0.03% $^{13}$C and $\sim 100\%$ $^{13}$C en-
riched diamonds were synthesized by high-pressure high-
temperature (HPHT) method using getters preventing incor-
poration of nitrogen into lattice. In all samples the con-
centration of paramagnetic impurity measured by ESR
was under detection limit (below 1 ppb) except 0.03% and
100% $^{13}$C diamond where the concentration of nitrogen was
at 1 ppm. 14

NV centers with different numbers of $^{13}$C atoms in the
immediate vicinity of the electron spin have been investi-
gated in $8.4\%$ $^{13}$C diamond. Figures 1(a)–1(d) show single
ESR spectra indicating the hyperfine coupling (HFC) of the
electron spin to zero, one, two, and three nuclear spins in the
first shell [Fig. 1(h)]. A magnetic field of $\sim 83$ G was or-
ented along the NV axis ([111]-axis). To characterize the spin
quantum states associated with the transitions in Figs.
1(b)–1(d), the spectra were simulated by exact diagonaliza-
tion of the spin Hamiltonian

$$H = g_e \beta_e \tilde{S}B + \tilde{S}D + (\tilde{S}A'I - g_n \beta_n I'B).$$

Here the electron spin $S = 1$ and $^{13}$C nuclear spins in first
shell are taken into account. $\beta_e$ is the Bohr and $\beta_n$ is the
nuclear magneton, respectively. Reported values for zero-
field splitting (ZFS) parameter $|D| = 2.87$ GHz, 15 isotropic
electron and nuclear Zeeman $g$ values ($g_e = 2.0028, g_n$
= 1.40483), and HFC parameters of $A_0 = 205$ MHz and $A_1$
= 123 MHz (Ref. 16) with angle of 106° between principal
axes of ZFS and HFC yield precise fits of the experimental
spectra. The small splittings in the central signals of the
spectra in Figs. 1(c) and 1(d) are explained by a second-order
perturbation approach. 3 The smaller amplitudes in higher fre-
hquency are due to absorption of MW by wire on the sample.

In the ESR spectra of $8.4\%$ $^{13}$C diamond, basically two
types of couplings are immediately visible [Figs. 1(b)–1(g)];
those around 130 MHz originating from first shell $^{13}$C and
those around 14 MHz. In C$_{3v}$ symmetry, the number of
equivalent atoms in close shells around NV is 3 or 6. In
recent theoretical study, 17 the 14 MHz splittings are assigned
to $^{13}$C at 3 and 6 equivalent sites in the third shell (see video
in Ref. 18). From measuring more than 250 individual cen-
ters and comparing the probability to find the 14 MHz split-
ting with the one predicted from theory we assign this split-
ting to nuclei in the third shell. 18

Individual nuclei in the spin cluster around the electron
are addressed via their particular NMR frequency. Given the
increase in spectral density apparent from Fig. 1 one might
wonder how far individual nuclei remain addressable. How-
ever, coherent control even in dense spin clusters remains
feasible as demonstrated in Fig. 2. Even in cases where there
are three $^{13}$C in the first shell, i.e., in total four qubits, Rabi
nutations of single nuclear spins can be driven by an addi-
tional RF as shown in Fig. 2(a). That is because even mul-
tiple RF transition frequencies originating from nuclei at
equivalent positions split due to higher order HFC contribu-
tions as shown above. The selectivity is not limited to the
relatively large splitting in the first shell but can be applied to
$^{13}$C nuclear spins in the third shell. A spectrum of single NV,
which has one $^{13}$C in the first shell and one $^{13}$C in third shell,
is shown in Fig. 1(g). We labeled the four nuclear spin states
as $|00\rangle$, $|01\rangle$, $|10\rangle$, and $|11\rangle$ as shown in Fig. 2(a). Rabi oscil-
lations between $|00\rangle$ and $|01\rangle$ could be observed as shown in
Fig. 2(d). To obtain a similar Rabi frequency for $^{13}$C nuclear
spins in the third shell as for those in the first shell, about
$1 \times 10^2$ times higher RF power was necessary. This
can be interpreted mainly by hyperfine enhancement, 19 which
predicts that Rabi frequency is almost proportional to HFC
and the square root of the RF power. A ten times smaller
HFC in the third shell supports this interpretation. A figure

![FIG. 2. (Color online) (a) Energy levels for nuclear spins in $M_z = -1$. Rabi oscillation of single $^{13}$C in the first shell of neighbors around the NV with (b) two $^{13}$C in the first shell and (c) three $^{13}$C in the first shell. (d) Rabi oscillation of single $^{13}$C in the third shell with one $^{13}$C in the first shell and one $^{13}$C in the third shell. The pulse sequence is $\pi$-MW-Rabi(RF)-$\pi$(MW) (Ref. 1). The ESR transitions of the MW $\pi$ pulse are those at lowest frequency in Figs.
1(c) and 1(d). (e) Elective nuclear double resonance (ENDOR) spectrum of $^{13}$C at first shell in (b) with fitted Gaussian line (blue dashed line) by the pulse sequence of $\pi$-MW(-RF)-$\pi$(MW). Free-induction decay (FID) of (f) $^{13}$C$^{-}$, (g) $^{13}$C$^{-}$, and (h) nuclear coherence between $|00\rangle$ and $|10\rangle$. (i) Pulse sequence for $^{13}$C$^{-}$ generation and detection between two nuclear spins, $E$ and $N$, marks the electron and the
two nuclear spins, respectively. Spin selective pulses are repre-
sented by squares, operating on a target qubit. Vertical lines rep-
sent logical connections. The control qubit state $|1\rangle$ and the state $|0\rangle$ are displayed as filled (●) and open (○) circles. For example, (○) indicates that the pulse is applied to the target qubit if the quantum state of the controlling qubit is $|0\rangle$.](image)
merit that characterizes the quality of coherent control was derived by swapping quantum states among individual nuclei. It was estimated by transferring polarization back to a detectable electron-spin state that 82 ± 5% of polarization was transferred from \(|00\rangle\) to \(|01\rangle\) for \(^{13}\)C nuclear spins in the third shell.

We are now in a position to engineer simple quantum states in the spin cluster around the electrons spin. Bell states \(\Phi^\pm = \frac{1}{\sqrt{2}} (|00\rangle \pm |11\rangle)\) and \(\Psi^\pm = \frac{1}{\sqrt{2}} (|01\rangle \pm |10\rangle)\) can be generated from the four effective nuclear spin states in Fig. 2(a). In the present case they were prepared from two \(^{13}\)C spins at the first shell. The procedure follows previous studies\(^2,2^0\) and is schematically shown for \(\Phi^+\) in Fig. 2(k).

After its generation, \(\Phi^+\) shows a FID, which is made coherent with an entanglement detector sequence [Fig. 2(k)]. In 8.4% \(^{13}\)C diamond, the free-induction-decay times \(T_2^\rho\) of \(\Psi^-(T_2^\psi)\) and \(\Phi^- (T_2^\phi)\) were estimated to be 22.0 ± 3.0 \(\mu\)s and 13.3 ± 1.1 \(\mu\)s, [see Figs. 2(f) and 2(g)] respectively, by fitting with exp\((-t/T_2^\rho)^2\cos(\Delta\omega t)\)\(^3\) where \(\Delta\omega\) is the detuned frequency of FID. As expected from the view point of decoherence free subspaces, \(2^1\) a longer \(T_2^\rho\) compared to that of \(T_2^\phi\) is observed.

The difference among \(T_2^\rho\) and \(T_2^\psi\) is best analyzed when compared with \(T_2^\phi\) of a nuclear quantum coherence among states \(|00\rangle\leftrightarrow|10\rangle\) and \(|00\rangle\leftrightarrow|01\rangle\). Those coherences are labeled as single-quantum coherences SQ1 and SQ2, respectively. Their \(T_2\) are measured to be \(T_2^{\text{SQ1}} = 41.1 \pm 3.1\) \(\mu\)s and \(T_2^{\text{SQ2}} = 15.8 \pm 1.4\) \(\mu\)s, respectively [Figs. 2(h) and 2(i)]. The difference of \(T_2^{\text{SQ1}}\) and \(T_2^{\text{SQ2}}\) might be caused by a spatially inhomogeneous magnetic noise around the defect caused by an inhomogeneous distribution of \(^{13}\)C around the two \(^{13}\)C in the first shell. Each spin-spin interaction between nuclear spin \(k\) surrounding the two \(^{13}\)C in the first shell with quantum numbers \(m_{1l}\) and \(m_{l2}\) causes oscillation given by \(\sum\exp[-i(\Delta\omega m_{1l} + \Delta\omega m_{l2})t]\)\(^2\). Here \(\Delta\omega_1\) and \(\Delta\omega_2\) are spin-spin interaction frequencies of the two \(^{13}\)C in the first shell due to surrounding \(^{13}\)C nuclear spins. This implies that \(T_2^\psi\) and \(T_2^\phi\) can be approximated by \(1/T_2^\psi = 1/[T_2^{\text{SQ1}} - 1/T_2^{\text{SQ2}}]\) and \(1/T_2^\phi = 1/T_2^{\text{SQ1}} + 1/T_2^{\text{SQ2}}\), respectively. Inserting the measured values for \(1/T_2^{\text{SQ1}}\) and \(1/T_2^{\text{SQ2}}\), the results are \(T_2^{\text{SQ1}} = 25.8 \pm 0.7\) \(\mu\)s and \(T_2^{\text{SQ2}} = 11.4 \pm 1.0\) \(\mu\)s, respectively, in good correspondence with measured values.

Besides the effect of the nuclear spin bath on individual \(^{13}\)C spins the static interaction between the single NV electron spin and its environment for different \(^{13}\)C concentrations was investigated by measuring \(T_2\), i.e., the inhomogeneous ESR linewidth. It was observed that \(T_2\) increases, i.e., the linewidth narrows, with decreasing \(^{13}\)C concentration as shown in Fig. 3. In 0.03% \(^{13}\)C diamond, an extremely long \(T_2\) of 30 \(\mu\)s was found (see Fig. 3). In the low \(^{13}\)C concentration region (\(\leq 1.1\%\)), the linewidth \(W\) (full width at half maximum) is derived from \(T_2\) by \(W = 2\ln2/\pi T_2\). The corresponding 18 kHz linewidth is the narrowest ever observed for an electron spin in a solid material. In the high \(^{13}\)C concentration region (\(> 1.1\%\)), the linewidth is derived from fitting the ESR line of a single NV with a Gaussian lineshape. Average values are plotted as squares in Fig. 3(e).

A likely cause for the inhomogeneous ESR linewidth is HFC to \(^{13}\)C nuclear spins. In e.g., Si, the dependence of the inhomogeneous linewidth of P donors on \(^{29}\)Si well is fitted by the isotropic HFC \((\alpha)\) due to Fermi contact interaction with \(^{29}\)Si nuclear spins with a concentration \((f)\), \(W = 2\ln2/\sqrt{\sum_{l}(\alpha_l/2)^2}\)\(^2\)\(^3\)\(^4\) The sum runs over all nuclear spins \(l\). In Fig. 3(e), the solid line for high \(^{13}\)C concentrations is calculated by summing only over all the nine sites in the third shell with \(\alpha_l = 14\) MHz (see above for assignment of sites and HFC constants). It should be noted that contributions from \(^{13}\)C in the first shell were not considered in the linewidth calculations because they contribute to an observable splitting but not to the linewidth. As seen from Fig. 3(e), it fits the experimental results well for high \(^{13}\)C concentration.

For lower \(^{13}\)C concentration, experimental data deviate from this behavior. This is due to the fact that the probability that any \(^{13}\)C is located close to the NV center is getting small upon reduction in \(^{13}\)C concentration. Furthermore, the unpaired electron-spin density rapidly decreases with distance from the three dangling bonds around the vacancy. This is known from the HFC parameters\(^16,17\) which indicates that almost 100% spin density is localized on the C sites in the first and the third shells. That is why in this situation the most prominent contribution to the inhomogeneous linewidth is the weaker dipole-dipole interaction between electron spin and \(^{13}\)C nuclear spin at distant sites. The lower line in Fig. 3(e) is the linewidth

\[
W = \sqrt{(\mu_0 \mu_e \mu_n g_e g_n/4 \pi h)^2 (3.195 \times 10^{16} n)}
\]  

calculated from the second moment\(^25\) with more than 3000 lattice sites for each \(^{13}\)C concentration \((n)\). Contributions from \(^{13}\)C in the first and second shells are not considered. As seen from Fig. 3(e), \(W\) fits the experimental results in the low \(^{13}\)C concentration (\(\leq 1\%\)) quite well. Obviously at low \(^{13}\)C concentration the linewidth is dominated by dipole-dipole interaction.
The dephasing time $T_2$ of the electron spin is measured by two pulse Hahn echo decay curves [Figs. 4(a)–4(c)]. We analyzed $T_2$ of the diamond made by CVD and excluded the 0.03% and 100% $^{13}$C diamond made by HPHT because paramagnetic impurities could not be suppressed in HPHT. In the 1.1% $^{13}$C diamond, a $T_2$ of 0.65 ms was found, which is the longest $T_2$ in diamond with natural abundance of $^{13}$C measured so far. For the lower $^{13}$C concentration of 0.3% an even longer $T_2$ of 1.8 ms was reported recently and added for the analysis. $T_2$ is found to be inversely proportional to the $^{13}$C concentration as plotted in Fig. 4(d).

In a theoretical analysis of $T_2$ by the disjoint cluster approach,\(^5\) the relationship of $T_2 \sim (\overline{C} n)^{-1/2}$ is proposed, where $\overline{C}$ is the averaged nuclear-nuclear dipolar interaction in the bath and $A_c$ is some characteristic value for the electron-nuclear dipolar interaction. Since both interactions scale linearly in $^{13}$C concentration ($n$), $T_2$ decreases approximately as $1/n$ in this model. The fitted line to the data shown in Fig. 4(d) supports this inverse proportionality and fits our data. Note that our data also fit the values calculated in (Ref. 5) within 30% deviation.

In conclusion, coherent control of up to three individual nuclei in a dense nuclear spin cluster is demonstrated. The $^{13}$C concentration dependence of $T_2^*$ and $T_2$ of electron spin point toward $^{13}$C nuclei as the main cause for dephasing in otherwise clean diamond. The correspondence with the theoretical line of $T_2$ (Ref. 5) is very important to elucidate the dephasing mechanism and to make $T_2^*$ longer for quantum information devices\(^4\) and ultrasupercryostat magnetometry.\(^6,7\) Furthermore, the results show that the threshold ($\sim 10^4$ operation) for quantum error-correction schemes\(^27\) can be exceeded even in $^{13}$C enriched diamond at room temperature with typical single-qubit flip of several ns.

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\(18\) See EPAPS Document No. E-PRBMD0-80-R14928 for the assigned sites of $^{13}$C at the third shell. For more information on EPAPS, see http://www.aip.org/pubservs/epaps.html.
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