Theoretical calculation for the ultraviolet optical properties of single-walled carbon nanotubes

Yoshiberu Takagi and Susumu Okada

Center for Computational Sciences and Graduate School of Pure and Applied Sciences, University of Tsukuba, Tsukuba 305-8571, Japan
and CREST, Japan Science and Technology Agency, 4-1-8 Honcho, Kawaguchi, Saitama 332-0012, Japan

(Received 25 March 2009; revised manuscript received 19 May 2009; published 19 June 2009)

We present a theoretical study of the ultraviolet (UV) optical properties of carbon nanotubes based on the local-density approximation in density functional theory and the generalized tight-binding approximation. Our calculations indicate that the absorption spectrum in the UV region depends strongly not only on nanotube diameter but also on chiral index. In zigzag nanotubes with even indices, peculiar features in the UV absorption spectrum emerge. In sharp contrast, these features are absent from the spectrum of zigzag nanotubes with odd indices. These spectral features are characteristic of interband transitions near the M point of the hexagonal Brillouin zone of graphene.

DOI: 10.1103/PhysRevB.79.233406 PACS number(s): 78.40.Ri, 71.20.Tx, 78.20.Bh

Carbon nanotubes have attracted significant attention from the pure and applied sciences due to their unique structural and electronic properties. One of the most fascinating aspects of nanotubes is that they exhibit either metallic or semiconducting electronic properties depending on their diameter and the atomic arrangement along their circumference. The unusual electronic properties of nanotubes open the possibility of fabricating superior nanometer-scale electronic devices in which the nanotubes would be a key constituent. For instance, it has been demonstrated that individual semiconducting nanotubes can work as field-effect transistors with properties that depend strongly on the nanotube species and the metal electrode species. Although knowledge of nanotube devices is steadily accumulating, difficulties in characterizing and extracting individual nanotubes slows the progress toward industrial applications.

For various applications, the use of nanotubes requires the characterization of the diameter and the chiral angle of each individual single-walled carbon nanotube. Optical spectroscopic techniques are one promising avenue for identifying and probing the geometric structure of nanotubes. The electronic structure of a nanotube, which is obtained by applying the discretization of the energy band of graphene, is directly affected by its atomic arrangement and diameter. Thus, careful investigation of the optical spectrum gives the geometric structure of individual nanotubes. Indeed, by comparing absorption spectra with electronic structures theoretically obtained, it is possible to identify not only the diameter but also the chiral index of each nanotube. The sensitive dependence of the low-energy (i.e., visible and near infrared) absorption spectrum on tube diameter has been experimentally demonstrated by Kataura et al. More recently, detailed ultraviolet (UV) spectroscopic experiments also clearly indicate that the spectrum depends strongly on tube diameter. However, to our knowledge, the calculation of the UV absorption spectrum is not yet addressed. Furthermore, the origin of the features in the UV spectra are still unclear.

The purpose of this Brief Report is therefore to explain theoretically the optical properties of nanotubes in UV region. To quantitatively discuss interband UV transitions we study the absorption coefficient of nanotubes in which the eigenstates are evaluated using the first-principle total-energy calculation in the framework of density functional theory (DFT). We also find more peaks in the absorption spectrum for zigzag nanotubes with even indices compared with that for zigzag nanotubes with odd indices [see Figs. 1(a) and 1(b)]. To complement the DFT results we also investigate the absorption coefficient for nanotubes with diameters less than

FIG. 1. (Color online) Absorption coefficients (α) in UV region for zigzag nanotubes (a) with even indices and (b) with odd indices calculated by using the LDA. Indices of nanotubes are listed in the right margin of each figure. Electronic structures of (c) the (10,0) nanotube and (d) the (9,0) nanotube. (e) Two-dimensional Brillouin zone with the hexagonal symmetry. M1, M2, and M3 indicate independent M point in the Brillouin zone. (f) Energy gap of zigzag nanotube with even indices at X point on their diameter.
14.0 Å. Our calculations indicate that peak shifts in the UV absorption spectrum also depends strongly on nanotube diameter as is the case for the low-energy absorption spectrum. The calculated shifts in the spectral peaks agree to an excellent degree with those observed experimentally. The results of the calculation indicate that the interband transition significantly affects the UV absorption spectrum of nanotubes.

To obtain one-electron states of individual nanotubes, we perform first-principle calculations using the local-density approximation (LDA) within the density functional theory. For the exchange-correlation energy between electrons, we use a functional fitted to the Monte Carlo results for a homogeneous electron gas. Norm-conserving pseudopotentials generated using the Troullier-Martins scheme are adopted to describe the electron-ion interaction. The valence wave functions are expanded using the plane-wave basis set with a cutoff energy of 49 Ry, making the relative total energies of carbon-related materials sufficiently convergent.

We adopt a supercell model in which a nanotube is situated with its wall separated from the walls of adjacent nanotubes by about 7.0 Å. The conjugate-gradient minimization scheme is utilized both for the electronic-structure calculation and for the geometry optimization. The lattice-parameter c is fixed during the structural optimization. In the optimized geometry, atoms are subjected to a force of less than 0.001 Hartree/a.u. integration over the one-dimensional Brillouin zone is carried out using the eight k points. The actual calculations were carried out using the Tokyo ab initio program package (TAPP).

In addition to the LDA in DFT we also use the tight-binding approximation to obtain the comprehensive electronic structure of the nanotubes. Here, 2s and 2p states of the carbon atom are used as the basis set to discuss the π-σ rehybridization induced by the nanotube curvature. Transfer and overlap integrals between neighboring atomic orbitals are suitably distance dependent in order to reproduce the electronic band structure for not only occupied states but also unoccupied states of various atomic configurations of the carbon atom. Furthermore, the nonorthogonality of the atomic orbitals on neighboring sites is fully taken into account. We set the cutoff radius to 4.0 Å in the tight-binding parameter set.

The absorption coefficient of the nanotubes, α(ω), is evaluated by calculating

\[ \alpha(\omega) = \frac{4\pi^2}{\omega V} \sum_{c,k'} \sum_{\epsilon_c(k')} |\langle k'|c|\epsilon_p(k)\rangle|^2 \delta(\epsilon_c(k') - \epsilon_e(k) - \omega), \]

where e is the light polarization vector, p is the electron momentum, V is the unit cell volume, ω is the photon energy, \( \epsilon_e(k) \) and \( \epsilon_c(k) \) are one-electron energies at momentum k for valence and conduction band electrons, respectively, and \( |k,c\rangle \) and \( |k,v\rangle \) are eigenstates in the valence and conduction band, respectively. In this work, we focus on optical interband transitions with the light-polarization vector parallel to the tube axis.

Figures 1(a) and 1(b) show the optical absorption spectra calculated using the LDA in the DFT of zigzag nanotubes possessing even and odd indices, respectively. We find clear features at about 4 and 5.5 eV in the absorption spectrum of zigzag nanotubes with even indices [Fig. 1(a)]. These features are found only for the even-index nanotubes and are absent from the absorption spectrum of zigzag nanotubes with odd indices [Fig. 1(b)]. We expect that the differences in the absorption spectra of nanotubes with even or odd indices reflect the electronic structure of individual nanotubes since absorption spectra are determined by energy-band dispersion.

To elucidate this issue, we focus on the electronic structure of zigzag nanotubes. In Figs. 1(c) and 1(d) we show the electronic structure of zigzag nanotubes with chiral indices (10,0) and (9,0), which are chosen as representative of zigzag nanotubes with even and odd chiral indices. By comparing these two electronic structures, we find a substantial difference at 2 eV above and below the Fermi level, where a pair of relatively flat dispersion bands [indicated by arrows in Fig. 1(c)] appear in the electronic structure of the (10,0) nanotube. No such state is present for the (9,0) nanotube [Fig. 1(d)]. The flat dispersion bands arise from the energy band of π and π* electrons along the two adjacent M points, \( M_2 \) and \( M_3 \), in the two-dimensional Brillouin zone of graphene [see Fig. 1(e)].

Analysis of the (10,0) nanotube band structure reveals the origin of the characteristic two-peak structure of the absorption spectrum of zigzag nanotubes with even indices, which comes from the interband transition between the π and π* bands at the X and Γ points, where they have relatively flat dispersion, resulting in the high- and low-energy features, respectively. Thus, the UV absorption spectrum exhibits spectral features that are characteristic of nanotubes with odd or even chiral indices.

In addition to the features in the UV absorption spectrum depending on chirality, we also find that they are sensitive to nanotube diameter. As clearly shown in Fig. 1(a), the absorption peaks near 4.0 and 5.5 eV shift to higher energy with increasing nanotube diameter. The blueshift reflects the modulation of energy gap between the π and π* bands at the X and Γ points, where they have relatively flat dispersion, resulting in the high- and low-energy features, respectively. Thus, the UV absorption spectrum exhibits spectral features that are characteristic of nanotubes with odd or even chiral indices.

Our DFT calculations for zigzag nanotubes indicate that the interband transition is responsible for the significant features in the UV absorption spectrum. To complement the results obtained by first-principle calculations, we use tight-binding calculations to study the absorption spectrum of carbon nanotubes of with diameters less than 14 Å. Figure 2 shows the absorption coefficient as a function of energy calculated using the tight-binding approximation for (10,m) and (9,m) nanotubes. We find that the UV spectral features allow the separation of the spectra into four classes. The first class contains the (10,m) nanotubes with even index m, which
The UV absorption spectra on nanotube diameter is at least partly caused by the interband transition at and around the $M$ point of graphene.

In summary, using both first-principle and tight-binding calculations, we study the UV optical properties of carbon nanotubes. For zigzag nanotubes with even indices, our first-principle calculations show two substantial features in UV region, whereas these features are absent from the absorption spectrum of zigzag nanotubes with odd indices. These features arise from interband transitions between the relatively low-dispersion bands discretized from the $M$-$M$ lines in the hexagonal Brillouin zone of graphene. In addition, the features are found to shift to higher energy with increasing tube diameter. Tight-binding calculations also indicate that the peaks in the absorption spectrum originate from interband transitions near the $M$ point. Moreover, we find a dependence of the UV absorption spectrum on the parity of the chiral index. We expect that combining our results with the low-energy spectral signatures of the $3n \pm 1$ family will lead to a more accurate characterization of nanotubes.

We thank K. Yanagi and T. Saito for communicating their results prior to publication. This work was partly supported by CREST in Japan Science and Technology Agency and a
grant-in-aid for scientific research from the Ministry of Education, Culture, Sports, Science and Technology of Japan. Computations were performed on NEC SX series at the University of Tsukuba, at the Yukawa Institute of Theoretical Physics, Kyoto University, at the Cybermedia Center, Osaka University, at the Information Synergy Center, Tohoku University, and at the Research Center of Computational Science, Okazaki National Institute.

10 K. Yanagi and T. Saito (private communication).
26 M. Tsukada, Computer program package TAPP, University of Tokyo, Tokyo, Japan, 1983–2009.